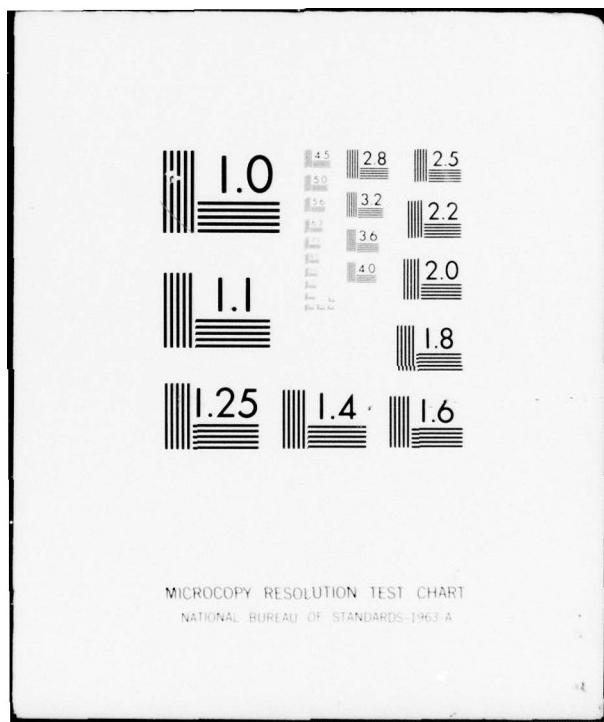


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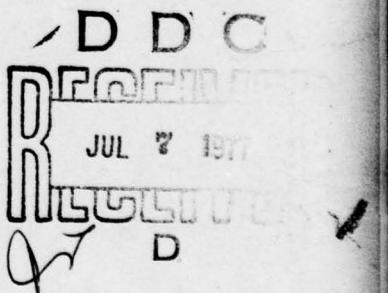
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COMMUNICATION SYSTEMS

by:

Gary E. Whitehouse  
John J. Fagan

Department of Industrial Engineering  
Lehigh University #19  
Bethlehem, PA 18015

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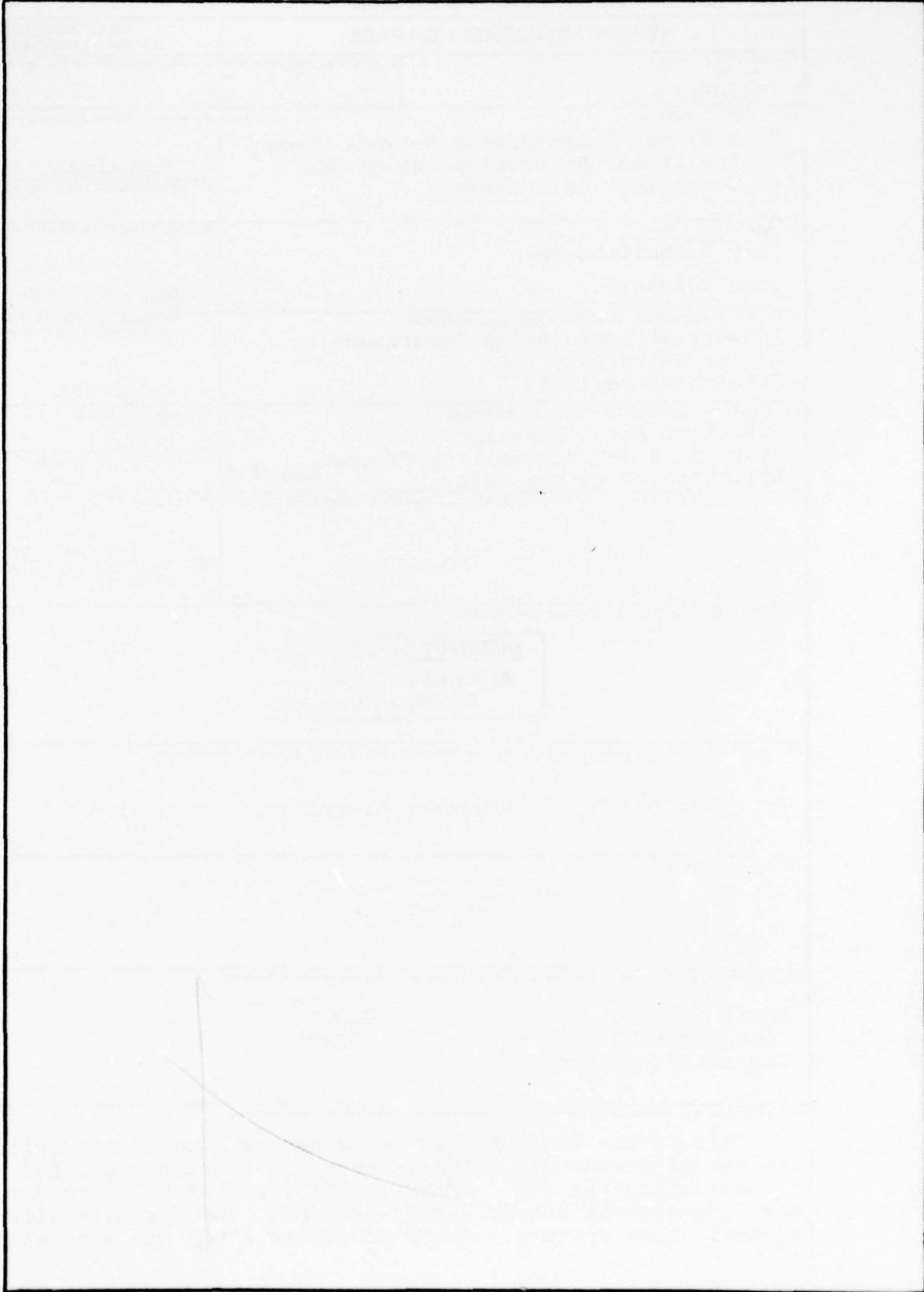
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## Introduction

Recent advances in computer-communications technology have given rise to the development of large, complex data communication networks. The high cost of developing and operating these networks have prompted researchers to search for appropriate measures of network performance. Techniques must be made available to analyze network design alternatives in terms of these performance measures. Researchers, however, have found it particularly difficult to develop analytical techniques that will effectively account for all of the complexities inherent in modern computer-communication networks. Consequently, many analysts have turned to simulation as an alternative. This report shows how certain simulation techniques can be used to estimate performance measures for various types of communication networks.

### Types of Communication Networks

Communication networks may be conveniently classified into three types as follows:

- (1) Circuit-Switched
- (2) Message-Switched
- (3) Packet-Switched

In circuit-switching, a "call" is set up between subscribers and message transmission takes place in a conversational mode. To set up the call, a path of connecting transmission lines must be established between source and destination. When one subscriber wishes to converse with another subscriber, a signal is transmitted through the network, seizing available channels in an attempt to reach the destination. If no path is available, a busy signal is returned to the caller who must then wait until the necessary channels are free. When a path has been established, message transmission takes place over all of the channels in the path in both directions simultaneously. The path remains allocated to the two subscribers until the caller releases the path or until the call is preempted by a subscriber of higher priority.

At the present time, circuit-switching is the most effective means of accommodating voice transmission, but it can also be used for transmission of data. A good example of a circuit-switched network is the public telephone system. Another is the AUTOVON network used by the Department of Defense for voice transmission.

In message-switching, transmission of data takes place in what is commonly known as a store-and-forward procedure. Unlike circuit-switching, only one channel is

used at a time for any given message transmission. The message first proceeds from its source to some other node in the network according to a predetermined routing algorithm. When the message arrives at this new node, it is either forwarded to the next node in its path or, if no channels are available, it is placed in a queue of messages awaiting transmission. The message proceeds through the network in this manner until it arrives at its destination. This way, a message only needs to occupy one channel at a time rather than an entire path from source to destination, thereby freeing channels for transmission of additional message. The AUTODIN network of the Department of Defense is a good example of a message-switched communication network. Many large corporations also use message-switched networks to satisfy their data transmission needs.

Packet-switching is very similar to message-switching in that it relies on a store-and-forward technique for transmission of messages. The difference, however, is that the messages are broken down at the source into small packets of a fixed size. The individual packets are then transmitted through the network in a manner similar to messages in a message-switched system. When all of the packets have arrived at the specified

destination, they are reassembled and the complete message is transmitted to the receiving subscriber. One of the main advantages of packet-switching is that many packets of the same message may be in transmission simultaneously. As a result, the transmission delay may be considerably less than with message-switching. This is known as the "pipelining" effect.<sup>1</sup> In some instances, transmission delays in a packet-switched environment have been found to be so low that the subscribers can exchange information in a manner similar to circuit-switched communication. The experimental ARPANET is an example of a packet-switched communication network.

Because of the technological and functional differences among the three types of communication networks, different measures are required to evaluate the performance of each type. A discussion of some of the relevant performance measures appropriate for each type of network is included in the following section.

#### Performance Measures for Communication Networks

Podell (15) has formulated a Measure of Effectiveness (MOE) to characterize the responsiveness of a digital system to any subscriber in a circuit-switched communication network. It is the probability that one of a

---

<sup>1</sup>Kleinrock, L., Queueing Systems, Volume II: Computer Applications, John Wiley and Sons, 1976, p. 294.

number of pre-specified subscriber-to-subscriber routes will:

1. be available (not failed in a long-term sense at the instant of demand)
2. not be blocked (by subscribers of equal or higher precedence fully occupying any portion of all of the pre-specified routes)
3. not fail in a long-term sense (over the subscriber's call interval)
4. not fail in a short-term sense (by providing an acceptably low probability of bit error over the call interval)
5. not be preempted (over the call interval by a subscriber of higher precedence)

The above joint probability statement is expressed as a sum of mutually exclusive terms, each term corresponding to one of the pre-specified routes through the network.

Podell and others created computer programs to determine the MOE in question in their development of ALAMO (6) and EVALMO (7). These computerized packages have been successfully used by the Defense Communications Agency to evaluate some of their existing and proposed communication systems. There is, however, one major deficiency in these packages and that is that the question of blocking and preemption were assumed to be negligible in these models. Fischer and Knepley (5) describe an algorithm

and a program which can be used to estimate the blocking probabilities by way of an interative procedure, given: the number of trunks in each trunk group of the network; the nodal originating-destination traffic requirements matrix in erlangs and the routing doctrine of the network. However, the work of Fischer and Knepley has not been integrated in the ALAMO and EVALMO packages. Simulation has been suggested as an alternate way of incorporating these particular results.

The store and forward communication networks require a different type of MOE than the one described above for circuit-switched networks. A message-switched or packet-switched network can be designed so that virtually all messages will be completed. This is accomplished by allocating sufficient storage space for the queueing of message at the various nodes in the network. Message queueing, however, can create a problem. If the system becomes overly congested, queues will become very large and the time to successfully transmit a message will increase accordingly. Message transmission time should therefore be a major component of a good measure of effectiveness for store-and-forward communication networks.

In many store-and-forward networks, message storage areas are large enough to insure that no messages will be lost as a result of balking from the message queues. In some instances, however, networks are designed in such a

way that a certain percentage of messages can be expected to balk from the queues during peak operation. This probability of balking should also be included in a measure of effectiveness for store-and-forward networks.

Podell's measure of effectiveness for circuit-switched networks can be used to accommodate message-switched or packet-switched networks if the following revisions are made:

1. The probability of a line being blocked is replaced by the probability of a message being lost as a result of balking from the message queue.
2. Message transmission time is included in the MOE. This can be accomplished by determining the probability that a message will be transmitted within a specified time. Different times might be specified for different precedence levels of messages.

The second and third chapters of this report are devoted to the use of a network simulation language known as QGERT to model message-switched and packet-switched communication networks respectively. The fourth chapter presents a GASP-IV program that can be used to model circuit-switched networks. The purpose of the modelling is to show how these techniques can be used to devise estimates of the performance measures described above. The following two sections contain a brief discussion of the background of QGERT and the symbols and terminology

required to understand the way in which it operates.

#### Background of QGERT

QGERT is the most recent in a series of programs developed to analyze GERT-type stochastic networks.

GERT was the result of research which effectively extended the work in PERT and CPM. Eisner and Elmagrahby suggested and experimented with additional node and arc logic which would allow for general precedence relationships and probabilistic structure in the network (2,3). Pritsker, Happ and Whitehouse (16,18,20) developed this idea further and defined the stochastic network or GERT network. Stochastic networks are characterized by:

1. Directed arcs representing activities or processes,
2. Each arc is assigned a probability of occurrence and other parameters which describe the distribution of time to traverse the network,
3. Logical nodes which denote the precedence relationship between the incident and emanating arcs of the node, and
4. The realization of the network is a set of arcs or nodes which define the path through the network for one experiment.

Initial work revolved around the analytical solution of GERT networks but after a time the networks became

more complicated and simulation approaches were used. There have been a number of computer packages which have been used effectively in the modelling of GERT type networks. These include:

1. GERTS IIIQ - This special version of GERTS analysis allows for the formulation of problems including Q-nodes. The queueing nodes allow for the modelling of systems which have store and forward features and seem to be effective for modelling some of the more advanced communication systems.
2. GERTS IIIQR - Hogg et al. (8,9,12) have developed a version of GERTS which combines the features of GERTS IIIQ and another model GERTS IIIR, which allows for the modelling of resource allocation considerations into the GERT model. Hogg et al. present a number of examples of their model which seem to be similar to the communication networks approach.
3. QGERT - This was developed by Pritsker (19) as an extended GERTS IIIQ. It accommodates much more advanced queueing logic than was previously available, making it very attractive for modelling fairly complex store-and-forward communication networks. Pritsker is also working on a new ver-

sion of QGERT which was not yet available at the time of this writing.

#### QGERT: Symbols and Terminology

QGERT is a network modelling technique and a high-level simulation language. The use of QGERT consists of the following two steps:

1. A network model of the system being studied is constructed using the various QGERT symbols.
2. Statistical quantities are derived from the model by using a "canned" computer program called Q-GERTS.

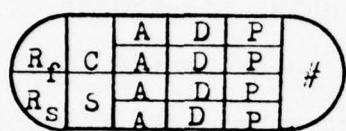
A detailed description of the QGERT modelling technique and the Q-GERTS simulation program can be found in the Q-GERTS User's Manual (19).

In general, a QGERT network consists of a series of nodes and branches. Special symbols are used to model the flow of transactions through the network. The flow of transactions involves: the releasing of nodes representing milestones or events; the performance of activities represented by branches of the network; the storing of transactions at Q-nodes awaiting processing by service activities; the branching of transactions through the network based on past and present conditions within the network; and the collection of statistical information concerning the transactions and the release times of nodes.

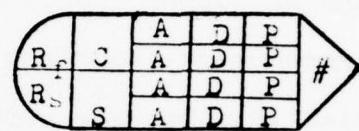
Some of the important QGERT symbols are shown in Figures 1 through 3. Most of the nodes in a QGERT network are regular nodes such as the ones shown in Figure 1. A regular node consists of an input side, a middle section and an output side. The input side shows the number of transactions required to release the node for the first time ( $R_f$ ) and the number required for subsequent releases ( $R_s$ ). The middle section is optional. It indicates the criterion for selecting attribute sets from incoming transactions (C); the type of statistics to be collected at the node (S); and the assignment of attributes to transactions passing through the node. Attribute assignment requires the specification of three values: an attribute number (A); one of the 15 distribution types provided in QGERT (D); and a parameter set number (P) indicating the parameters that are to be used in the selection of a value from the distribution specified. Multiple attribute assignments are permitted at a node. Each of the nodes in Figure 1 provides for four different attribute assignments. The output side of a regular node indicates the node number and the type of branching which is to occur from the node. The type of branching is indicated by the shape of the output side of the node. Figure 1(a) shows the symbol for deterministic branching. This means that all activities emanating from this node will be initiated. Probabilistic branching is indicated by Figure 1(b). Only

QGERT Symbols: Regular Nodes

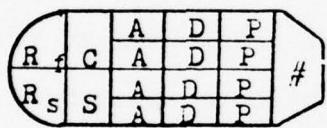
FIGURE 1.



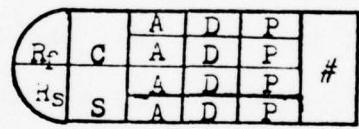
(a) Deterministic



(b) Probabilistic



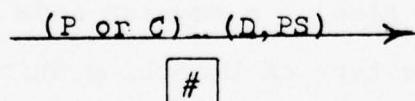
(c) Conditional-Take-First



(d) Conditional-Take-All

QGERT Symbols: Activities

FIGURE 2.



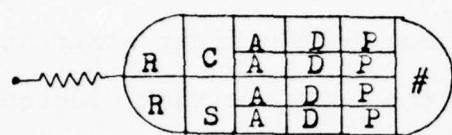
one activity emanating from this node will be selected. The selection is on a random basis according to the probabilities specified on the activities. The symbols for conditional branching are shown in Figures 1(c) and 1(d). QGERT provides 14 condition codes which can be associated with an activity. With conditional-take-first branching, the activities emanating from the node are rank ordered. The conditions associated with the activities are tested in order. When one of the conditions is satisfied, that activity is initiated. For the case of conditional-take-all branching, the conditions for all activities emanating from the node are tested and each activity is initiated if its condition is satisfied.

The branches or activities in a QGERT network are represented in Figure 2. Each activity has associated with it a probability (P) if it emanates from a node with probabilistic branching, or a condition code (C) if it emanates from a node with conditional branching. The time to complete the activity can also be specified. The time can either be constant or it can be a value from a distribution (D) with parameter set (PS). An optional activity number may also be specified. If no time is specified, the activity duration will be zero time units.

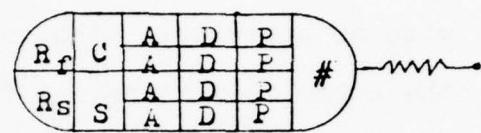
In addition to the regular nodes in a QGERT network, there are a few special-purpose nodes. These are shown in Figure 3. Figure 3(a) represents a source node.

QGERT Symbols: Special-Purpose Nodes

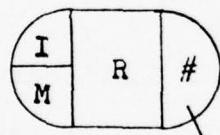
FIGURE 3.



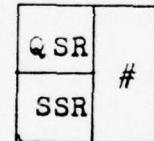
(a) Source Node



(b) Sink Node



(c) Queue Node

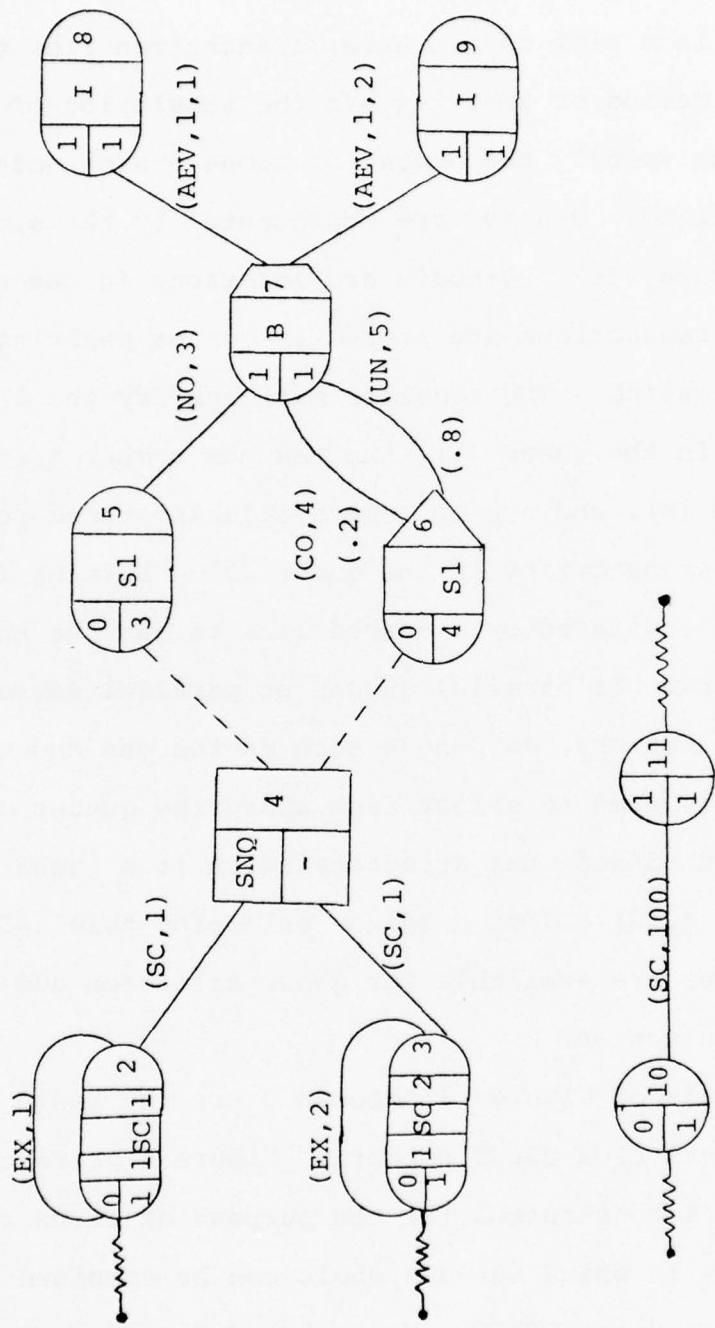


(d) Selector Node

These are the nodes at which transactions are created.

Figure 3(b) is a sink node. Here, transaction flow terminates. One method of shutting off the simulation of the network is to specify the number of times a sink node must be realized. Q-nodes are represented by the symbol shown in Figure 3(c). Q-nodes are locations in the network where transactions are stored in queues awaiting further processing. The modeller must specify the initial number in the queue (I), the maximum number permitted in the queue (M), and one of four available procedures for ranking transactions in the queue (R). Balking from the queue is indicated by a dashed line to another node in the network. If parallel queues or parallel servers exist in the network, an S-node such as the one shown in Figure 3(d) is used to select from among the queues or servers. Each S-node has associated with it a queue selection rule (QSR) and/or a server selection rule (SSR). Fourteen rules are available for queue selection and eight for server selection.

The symbols of Figures 1 through 3 are the basic building blocks of a QGERT network. Figure 4 presents a sample network constructed for the purpose of illustrating the ways in which these symbols can be combined to model a system using QGERT. Nodes 2 and 3 represent source nodes. A constant value of 1 is assigned to attribute 1 in node 2, and a constant value of 2 is assigned



A Sample QGERT Model

FIGURE 4.

to attribute 1 in node 3. The branches looping back on nodes 2 and 3 represent the time between arrivals of transactions. The interarrival times are exponentially distributed with parameter sets 1 and 2. The activities from nodes 2 to 4 and 3 to 4 each have a constant duration of 1 time unit. Node 4 is an S-node which sends transactions to one of the parallel queues represented by Q-nodes 5 and 6. The queue selection rule is SNQ. This implies that the S-node will select the queue which currently contains the smallest number of transactions. Q-node 5 allows a maximum of 3 transactions and Q-node 6 allows a maximum of 4. The ranking procedure in both queues is S1, meaning that transactions with the smaller values of attribute 1 will be ranked ahead of those with larger values of attribute 1. The duration of the service activity from node 5 to node 7 is normally distributed with parameter set 3. Q-node 6 has probabilistic branching. The network model indicates that 20% of the transactions will be serviced in a constant time with parameter set 4 and 80% of the transactions will be serviced according to a uniform distribution with parameter set 5. At node 7, statistics are collected on the time between successive realizations of the node. Branching from node 7 is conditional-take-first. Transactions with attribute 1 equal to 1 will be sent to node 8 and transactions with attribute 1 equal to 2 will be sent to node

9. Statistics are collected at nodes 8 and 9, showing the interval of time elapsed since the transaction was last marked. Transactions are automatically marked at source nodes. Since no other marking was indicated in the network, the statistics collected for nodes 8 and 9 will represent the time elapsed between the departure of a transaction from a source node until its arrival at nodes 8 and 9 respectively. Nodes 10 and 11 form a disjoint part of the network sometimes referred to as a "simulation clock." Node 10 is a source node and node 11 is a sink node. The activity between nodes 10 and 11 has a duration of 100 time units. When 100 time units have elapsed, sink node 11 will be realized and the simulation will be terminated.

#### The Q-GERTS Computer Program

After a system has been modelled using the symbols described in the previous section, the Q-GERTS computer program is used to perform the desired network analysis. Q-GERTS is written in FORTRAN-IV and uses simulation to analyze QGERT networks. The Transition from the QGERT model to the Q-GERTS input is very simple. One data card is required for each node, activity, parameter set, and attribute assignment. An additional card is required to provide some general information about the network. The input is free-form, permitting data to be entered

without card column restrictions. Each card contains a three-letter identification to specify the symbol represented by the card and additional parameters to describe the symbol. All values on the card are separated by commas.

The output from the Q-GERTS program includes the following:

1. An echo check of the input.
2. A listing of the input cards.
3. Results of the first simulation of the network (optional).
4. A summary report for the total number of simulations performed. In addition to the statistics called for by the modeller, Q-GERTS provides statistics on: average number in each of the Q-nodes, average server utilization, and average number of transactions balking per unit time from each of the queues.
5. Histograms for each of the statistics collected (tabular or plotted).

The sample QGERT model described in the previous section was analyzed with the Q-GERTS program. The results for five simulations of the network can be found in Appendix A.

## MODELLING MESSAGE-SWITCHED COMMUNICATION

### NETWORKS WITH QGERT

A brief description of the concepts involved in message-switching was included in the introduction. Basically, messages are transmitted from node to node in the communication network in a store-and-forward manner. If all possible communication channels are busy, the message waits in a queue until one of the channels becomes available. This idea of storing-and-forwarding is what makes message-switched networks good candidates for QGERT analysis.

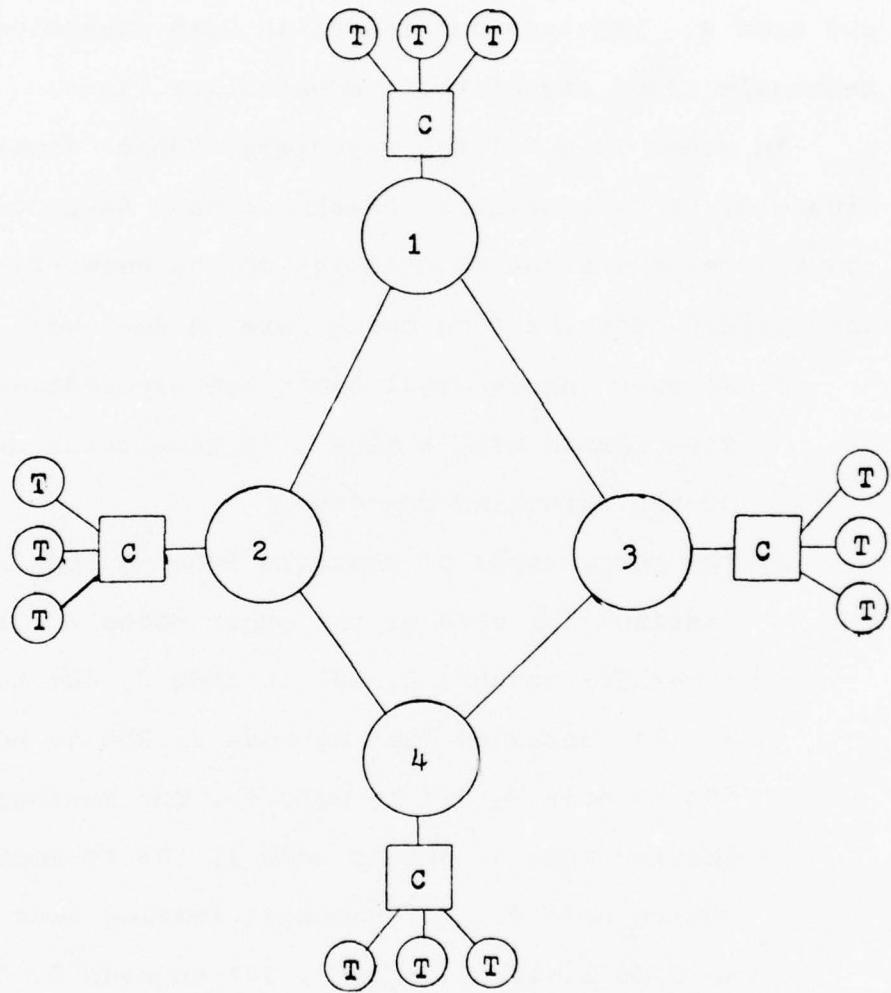
#### A Hypothetical Network

In order to demonstrate the use of QGERT to model message-switched communication networks, it was decided to use a simple hypothetical four-node communication network. If the concepts in modelling simple networks are understood, they can be easily extended to the modelling of large, fairly complex networks. The network selected for analysis is the one shown in Figure 5.

The nodes in the network of Figure 5 are numbered 1 through 4. The nodes actually represent switching centers that operate by means of message-switching. Each switching center has associated with it a computer (C)

Four-Node Communication Network

FIGURE 5.



and a system of terminals (T). A message originating at any one of the centers can be transmitted to any of the other centers. The network is fully connected except for the fact that there is no direct link between node 1 and node 4. Messages can travel in both directions simultaneously along any of the communication lines.

In order to model the message-switched network of Figure 5, it is necessary to make certain assumptions about some of the characteristics of the network. These assumptions, for the time being, are as follows:

1. Message interarrival times are exponentially distributed with a mean of 2 time units at each of the switching centers.
2. The percentages of messages leaving node 1 and destined for each of the other nodes are as follows: 30% to node 2, 30% to node 3, 40% to node 4. For messages leaving node 2: 30% to node 1, 40% to node 3, 30% to node 4. For messages leaving node 3: 40% to node 1, 30% to node 2, 30% to node 4. For messages leaving node 4: 30% to node 1, 40% to node 2, 30% to node 3.
3. There are 3 priority classes of messages. The breakdown is as follows: 10% are priority 1 (high priority); 30% priority 2; 60% priority 3. This distribution holds for all combinations of source and destination.

4. Message length (in terms of transmission time) is exponentially distributed with a mean of 10 time units for all types of messages.
  5. The times required to transmit a single bit of information along each of the communication links (a function of the length of the link) are as follows: 2.5 time units between nodes 1 and 2; 3.0 time units between nodes 1 and 3; 2.0 between 2 and 3; 1.0 between 2 and 4; 1.5 between 3 and 4.
  6. Queues are large enough so that no messages will be lost as a result of balking. The messages in the queues are ranked according to priority, but high priority messages do not preempt lower priority messages.
  7. Messages going from node 1 to node 4 are initially routed to node 3 and messages going from node 4 to node 1 are initially routed to node 2.
  8. Each of the communication lines in the network contains four channels for message transmission.
- With these characteristics in mind, a QGERT model of the four-node message-switched communication network of Figure 5 was developed. The following section explains the model in detail.

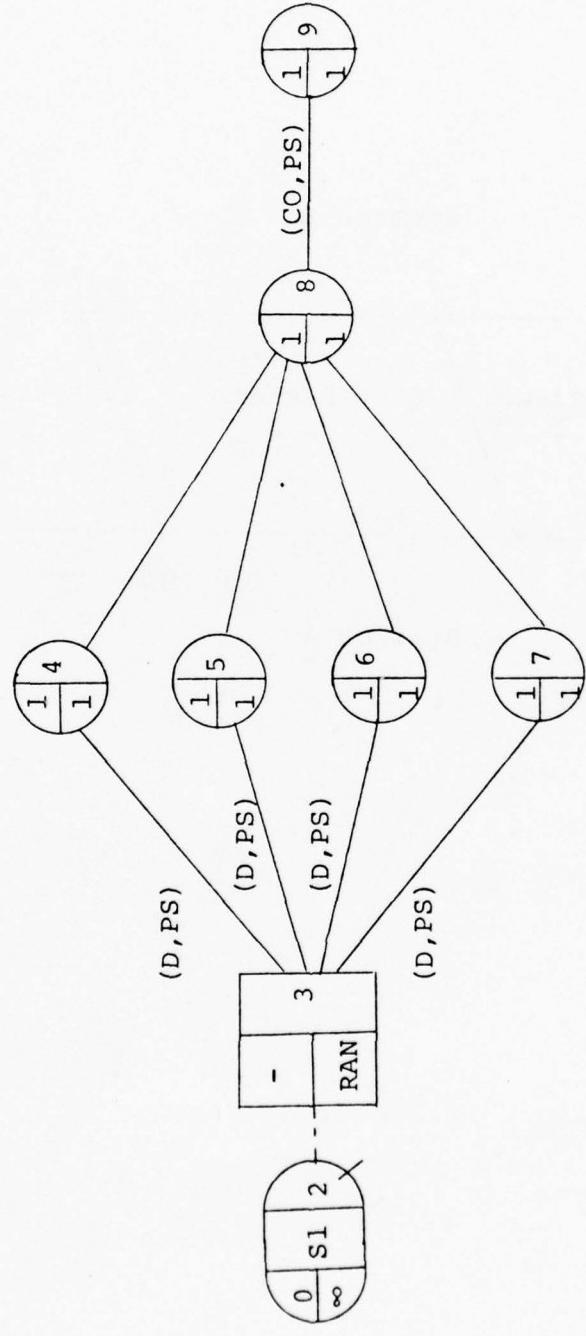
#### Development of the QGERT Model

The key to modelling a store-and-forward communication network is to think of a communication line as a

series of parallel servers. The parallel servers are the various communication channels in the line. The transactions that they serve are the messages that are being transmitted over the channels. Figure 6 depicts a sample communication line with 4 channels as it would be modelled using QGERT.

Node number 2 is a Q-node. It represents the storage area for messages awaiting transmission. Node 3 is an S-node. It selects from among the four communication channels in the line. The server selection procedure is random (RAN). This implies that if more than one channel is available for the transmission of a message, the available channels have an equal probability of being selected. The channels are represented by the activities from node 3 to nodes 4, 5, 6, and 7 respectively. Message transmission time is made up of two components. The first component is variable and is dependent on the message length. It is represented as a value from a distribution D with parameter set PS and is shown on the service activities emanating from node 3. The second component is fixed and is a function of the length of the communication line. It is represented on the activity between nodes 8 and 9 as a constant value with parameter set PS.

The principle of the two components of message transmission time is illustrated in Figure 7. Two messages are being sent from station A to station B.

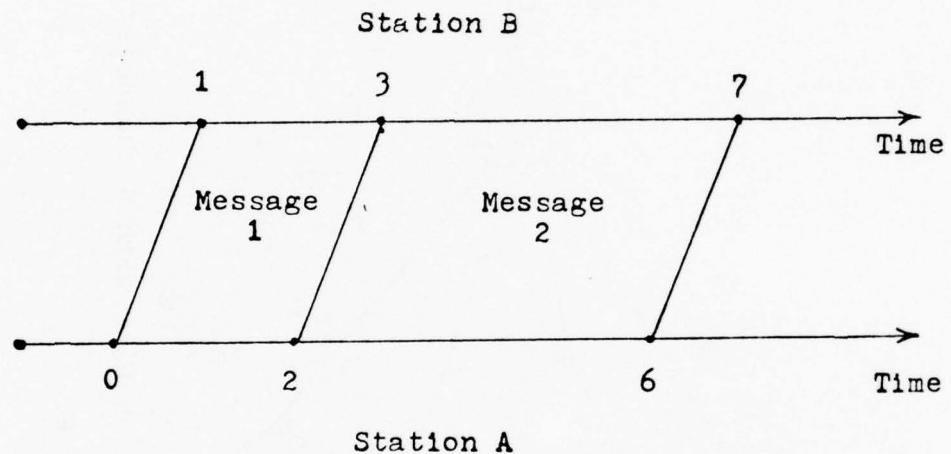


QGERT Model of a Communication Line with 4 Channels

FIGURE 6.

Two Components of Message Transmission Time

FIGURE 7.



Transmission of message 1 at station A begins at time 0 and ends at time 2 for a variable component of 2 time units. The fixed component of transmission time is 1 time unit so that station B begins to receive the message at time 1. Transmission of message 1 is completed when the last bits of information are received by station B at time 3. Total transmission time is 3 time units. Transmission of message 2 begins at time 2 and ends at time 6 for a variable component of 4 time units. Transmission is completed at time 7 for a total transmission time of 5 time units.

A QGERT model of a communication network is made up of three major parts. These parts can be categorized as follows:

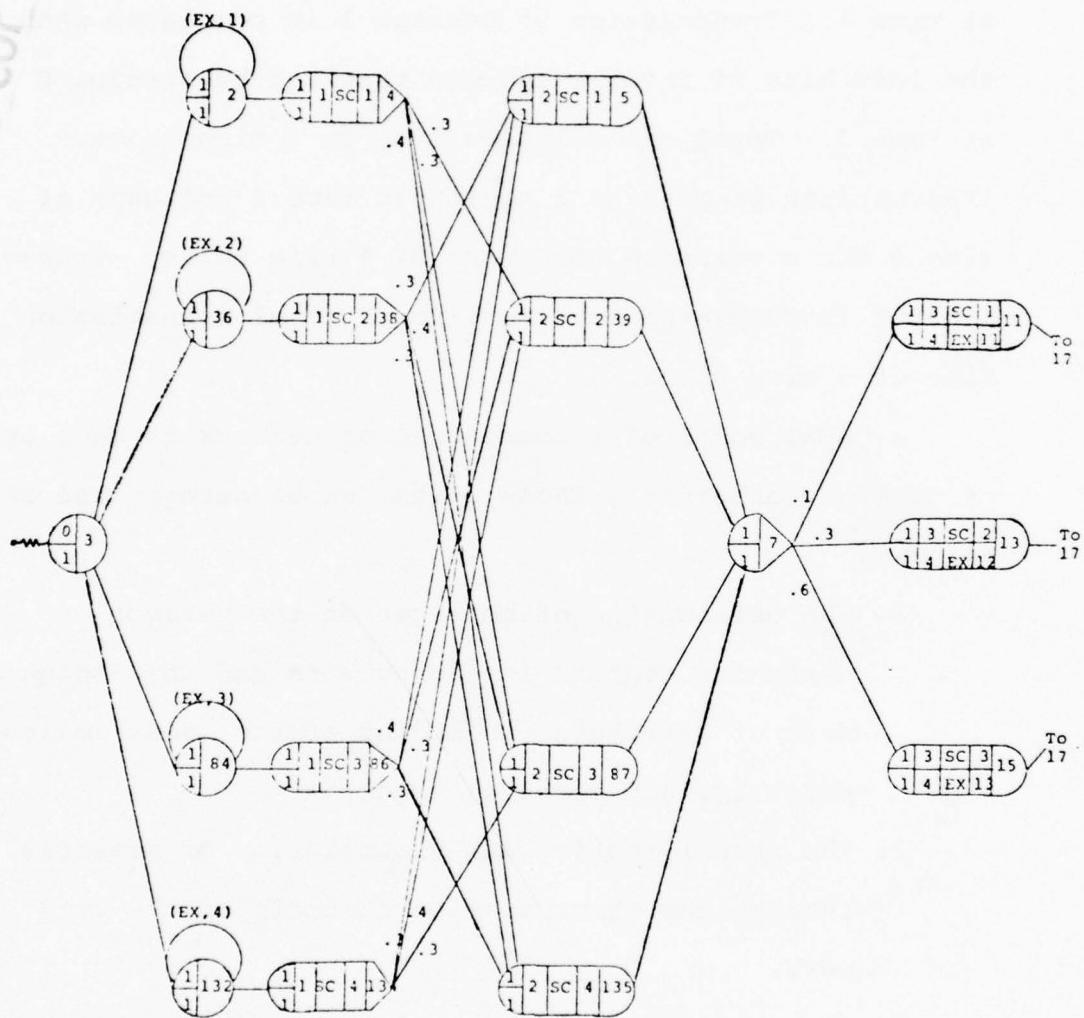
1. The origination of messages at the various switching centers in the network and the assignment of attributes including source, destination, priority, and message length.
2. The actual routing and transmission of messages through the communication channels of the network.
3. The collection of statistics describing the performance of the network.

The entire QGERT model of the four-node message-switched communication network of Figure 5 appears in Figure 8. Parts a, b, and c of Figure 8 correspond to

QGERT Model of a Four-Node Message-Switched Communication Network: Message Generation

FIGURE 8(a)

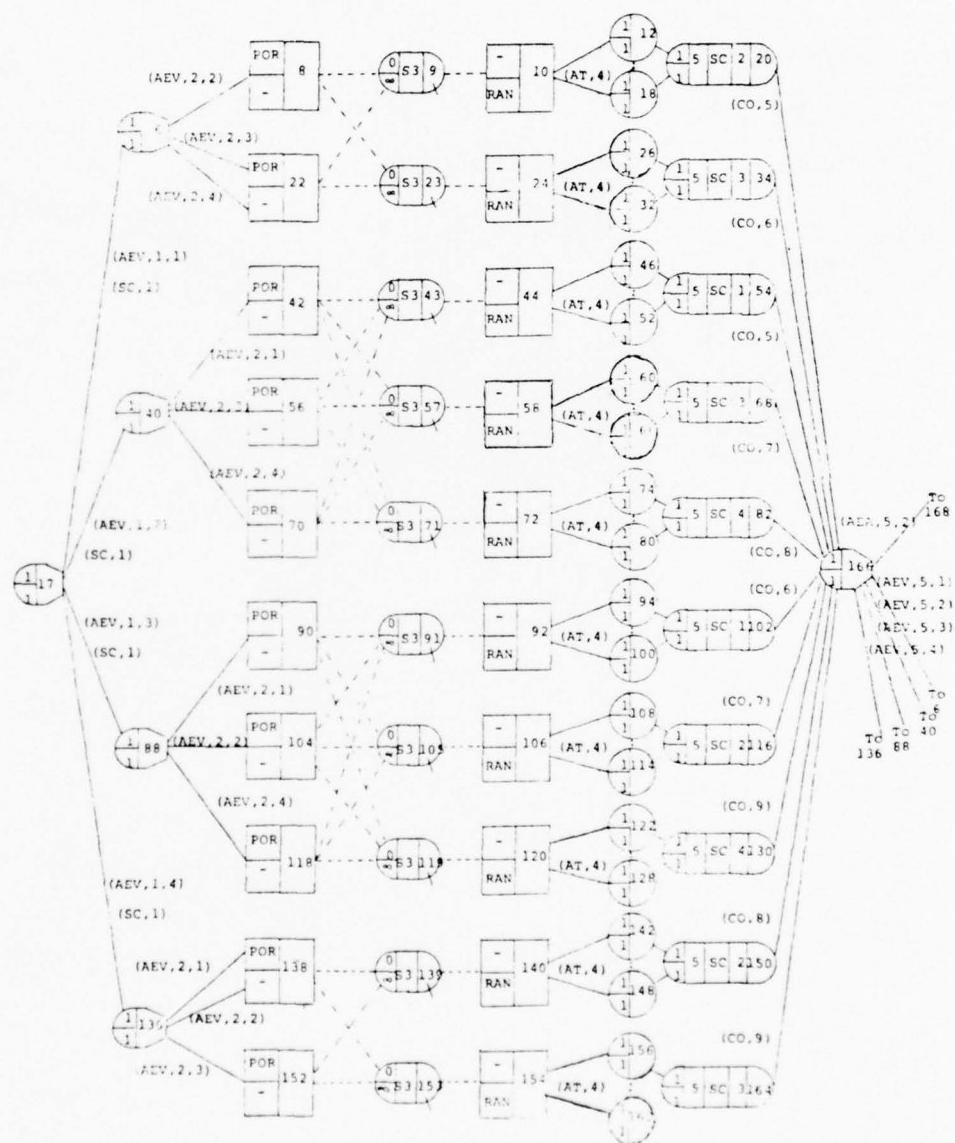
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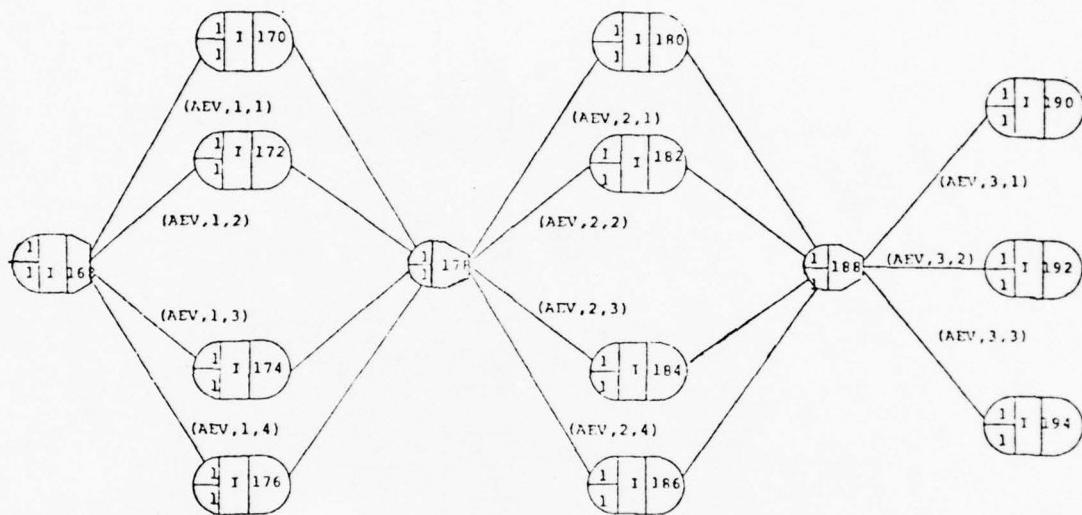
## QGERT Model of a Four-Node Message-Switched Communication Network: Routing and Transmission

FIGURE 8(b)



GGERT Model of a Four-Node Message-Switched Communication Network: Statistics Collection

FIGURE 8(c)



the three parts of the model as described above. The remainder of this section is devoted to an explanation of the model.

Nodes 2, 36, 84, and 132 represent the four switching centers in the network where messages originate. The activities looping back on these nodes represent the time between arrivals of messages. Interarrival times are exponentially distributed with a mean of two time units at each of the centers. The distribution of interarrival times can be easily modified by changing the values in parameter sets 1, 2, 3, and 4.

Values of attribute number 1 are assigned at nodes 4, 38, 86, and 134 indicating the origin of a message at stations 1, 2, 3, and 4 respectively. The branching from each of these nodes is probabilistic. The activities emanating from them show the probabilities of messages being sent to each of the other stations in the network (in accordance with the proportions stated in the description of the network in the previous section). The destination of a message is indicated by values assigned to attribute number 2 at nodes 5, 39, 87, and 135. The activities emanating from these nodes feed into node 7. Branching from node 7 is probabilistic also, with 10% of the transactions going to node 11, 30% to node 13, and 60% to node 15.

Values of attribute numbers 3 and 4 are assigned at nodes 11, 13, and 15. Attribute number 3 indicates the message priority level. A constant value of 1 is assigned at node 11, 2 at node 13, and 3 at node 15 indicating messages of high priority, middle priority, and low priority respectively. Attribute number 4 represents the message length in terms of transmission time. Transmission time is exponentially distributed with parameter set 11 for high priority messages, 12 for middle priority messages, and 13 for low priority messages. Initially, all three distributions have a mean of 10 time units (as specified in the network description).

Following the assignment of attributes 3 and 4, the message is sent to node 17 to determine where it should be routed for initial transmission. At this point, no time has elapsed since the origination of the message.

Branching from node 17 is conditional-take-first, based on the value of attribute 1. Messages from source number 1 (ie.: those with attribute 1 equal to 1) are sent to node 6; messages from source 2 are sent to node 40; messages from source 3 are sent to node 88; and messages from source 4 are sent to node 136. The activities emanating from node 17 all have a constant time of 1 associated with them. This is the time required to process the message prior to transmission. Branching from nodes 6, 40, 88, and 136 is also conditional-take-first, this

time based on the value of attribute number 2 (the destination of the message). Messages are routed from these nodes to an appropriate S-node in order to select a communication line for transmission. For example, a message with attribute 1 equal to 2 and attribute 2 equal to 3 will be initially routed to node 40 and then to S-node number 56. At this point, the message will be sent to one of three possible Q-nodes (43, 57, or 71) depending on the queue selection rule specified for the S-node. In this case, the queue selection rule for each of the S-nodes is POR which stands for "preferred order." The preferred order for messages going from source 2 to destination 3 is Q-node 57, followed by Q-node 71, followed by Q-node 43. Q-node 57 represents the queue of messages awaiting transmission over the link between stations 2 and 3; Q-node 71 represents the queue for the link between stations 2 and 4; and Q-node 43 represents the queue for the link between stations 2 and 1. Each of the Q-nodes in Figure 8(b) has an infinite queue length. Therefore, the queues will never be full and all messages going from station 2 to station 3 will be initially routed to Q-node 57. If, however, a limit was placed on the size of the queues and the queue for node 57 became full, a message going from station 2 to station 3 would have to be placed in the queue at node 71 and would initially be transmitted to station 4 before going on to station 3. If the queue

at node 71 was also full, the message would be placed in the queue at node 43 and would be transmitted to station 1 initially.

There are 10 Q-nodes in Figure 8(b). Each of the Q-nodes is followed by an S-node and a set of parallel servers, making up the symbol set for a communication link as was previously described in the explanation of Figure 6. There are 2 such sets of symbols for each of the 5 links in the communication network, representing the transmission of messages in both directions over the link. The ranking procedure for each of the queues is S3, meaning that messages are ranked according to attribute 3 with small values first. Attribute 3 was used to designate the priority class of the message. The activity times for the service activities are shown as (AT,4). This means that the time to complete the activity will be equal to the value stored in attribute 4 for each message. Attribute 4 was used to assign a value representing the variable component of the message transmission time. Each of the communication lines contains 4 channels. Because of limited space, however, Figure 8(b) only shows 2 channels for each of the lines. The other channels are indicated by a series of dots.

After a message has been transmitted over one of the communication lines, a value is assigned to attribute 5 indicating the station to which the message has just been

transmitted. The message is then sent to node 166. The times on the activities leading into node 166 represent the fixed component of message transmission time and correspond to the values given for each of the lines in the description of the network. Branching from node 166 is conditional-take-first. A check is made to see if attribute 5 is equal to attribute 2. If it is, the message has arrived at its destination and is ready to be sent to the statistics collection part of the network. If not, the message is routed back to node 6, 40, 88, or 136 (depending on the value of attribute 5) for further transmission.

When a message arrives at its destination, it is sent from node 166 to node 168 for statistics collection. Node 168 is a statistics node which calls for the collection of "interval" statistics. This is designated by the letter I in the central portion of the node. Statistics associated with node 168 on the Q-GERTS output will indicate the average time spent in the system for all messages. Branching from node 168 is conditional-take-first, based on attribute 1 (the source of the message). Interval statistics for nodes 170, 172, 173, and 174 will indicate the average time in the system for messages originating at stations 1, 2, 3, and 4 respectively. Next, messages are routed according to the value of attribute 2 (destination) to node 180, 182, 184, or 186 where

statistics will be collected indicating average time in the system for messages which have arrived at stations 1, 2, 3, and 4 respectively. Finally, messages are routed from node 188 to node 190, 192, or 194 where interval statistics are collected for the three priority levels of messages. Statistics for high priority messages are collected at 190; middle priority at node 192, and low priority at node 194.

The subnetwork consisting of source node 175 and sink node 173 is the simulation clock. The activity time for the branch connecting the two nodes indicates that the simulation is to be run for 300 time units. In the input to the Q-GERTS program, it will be specified that statistics collection is not to begin until 100 time units have elapsed. This permits the system to reach a steady-state before any statistics are collected. Statistics will therefore be collected over an interval of 200 time units.

#### Simulation Results

The Q-GERTS program was used to analyze the network described in the previous section. The input to the program consists of one card for each of the nodes, activities, parameter sets, and attribute assignments shown in Figure 8; and a card that contains some general information about the network being modelled. The information contained on this card includes the following:

1. A three letter ID to indicate that the card contains general information (GEN).
2. The name of the analyst.
3. The project number.
4. The date.
5. The number of sink nodes in the network (1).
6. The number of nodes for which statistics are kept (13).
7. The number of sink nodes to realize the network (1).
8. The number of simulations of the network (2).
9. An integer random number seed.
10. The maximum number of attributes associated with each transaction flowing through the network (5).
11. The time from which statistics will be kept (100.0).
12. The type of histogram desired (tabular).

The GEN card must be the first card in the input deck. It is followed by the cards representing the nodes, parameter sets, and attribute assignments. These can be arranged in any order and are followed by cards representing the activities in the network. The last card in the input deck contains the letters "FIN".

The results of 2 simulations of the network shown in Figure 8 are as follows:

1. Average message transmission times

<u>Message Type</u>	<u>Node No.</u>	<u>No. of Time Units</u>
Priority 1	190	12.3361
Priority 2	192	16.0297
Priority 3	194	19.3908
Source 1	170	27.2049
Source 2	172	12.3500
Source 3	174	14.0068
Source 4	176	17.1912
Destination 1	180	17.4733
Destination 2	182	13.2201
Destination 3	184	15.1907
Destination 4	186	25.4596
All Messages	168	17.7135

2. Average number in Message Queues

<u>Communication Link</u>	<u>Node No.</u>	<u>Avg. No. in Queue</u>
1 to 2	9	.0154
1 to 3	23	3.7137
2 to 1	43	.4964
2 to 3	57	.0655
2 to 4	71	.0000
3 to 1	91	.0552
3 to 2	105	.0047
3 to 4	119	2.1353
4 to 2	139	1.7557
4 to 3	153	.0958

### 3. Average Channel Utilization

<u>Communication Link</u>	<u>Activity No.</u> <sup>2</sup>	<u>Percentage Busy Time</u>
1 to 2	198	.2400
	197	.3546
	196	.3673
	195	.4055
1 to 3	194	.9067
	193	.9168
	192	.8631
	191	.9088
2 to 1	190	.6405
	189	.6398
	188	.6043
	187	.7193
2 to 3	186	.4684
	185	.5523
	184	.4080
	183	.4815
2 to 4	182	.3320
	181	.4038
	180	.2858
	179	.3909
3 to 1	178	.3933
	177	.4717
	176	.4371
	175	.5121

<sup>2</sup>The QGERTS program assigns activity numbers to service activities if none are specified in the program input.

3 to 2	174	.3530
	173	.3457
	172	.4700
	171	.3129
3 to 4	170	.7801
	169	.8230
	168	.8815
	167	.7987
4 to 2	166	.8115
	165	.8177
	164	.8731
	163	.9008
4 to 3	162	.4400
	161	.5247
	160	.4227
	159	.4256

A complete listing of the Q-GERTS input and output (which includes much more information than what is shown above) for this model can be found in Appendix B.

#### Modification of the Network

One of the interesting features of the QGERT modeling technique is the ease with which a model can be modified. For example, the interarrival time of messages at one of the stations in the communication network can be modified simply by changing the values on one card in the input desk. The same is true for such parameters as: activity times, probabilities of selecting among activities,

maximum queue lengths, attribute values, and queue or server selection rules. There are three major modifications that an analyst might wish to make to the model of the message-switched communication network shown in Figure 8. These are:

1. To limit the size of message queues and permit messages to "balk" from the system.
2. To allow for more generalized message generation.
3. To account for changes in the structure of the communication network.

The remainder of this section discusses the changes that must be made to the QGERT model in Figure 8 in order to implement these modifications.

#### 1) Limiting the size of message queues

The QGERT model discussed in the previous section permitted queues of messages to build up indefinitely. This insured that all messages would eventually be transmitted successfully. In reality, there must be some limit to the number of messages that can be allowed to accumulate in a storage area. If the maximum queue length is small, some of the messages will balk from the queues and will not be completed. In order to incorporate this idea into the QGERT model of a message-switched communication network, the following changes must be made to the model in Figure 8:

- a) The maximum number permitted in the queues must be changed from an indefinitely large number to whatever the actual maximum is.
- b) For each of the selector nodes, a node number must be specified to show where balkers are to be sent. If all of the queues associated with a particular S-node are full, an arriving message will balk to this specified node.
- c) The portion of the network model devoted to statistics collection must be revised to collect statistics on the messages that balk from the queues.

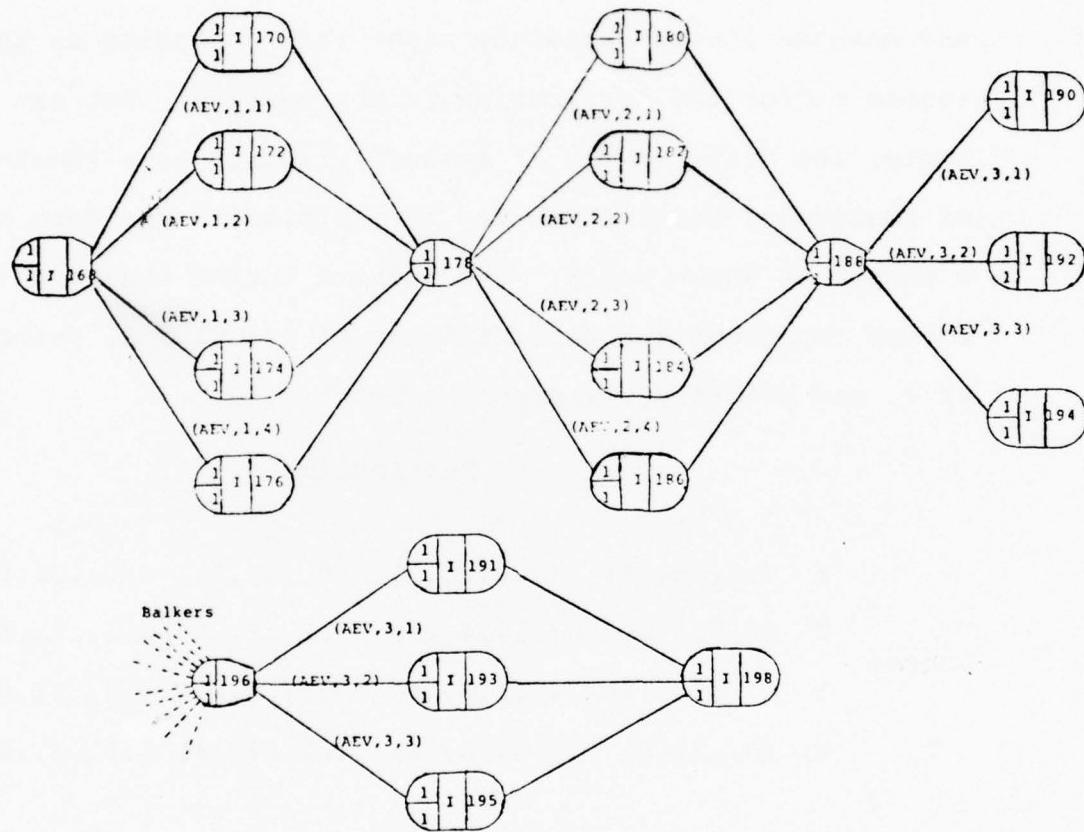
The Q-GERTS program was used to analyze a message-switched network similar to the one modelled in Figure 8 where the queues were limited to a maximum of 5 messages. The revised statistics section of the model is shown in Figure 9. All messages that balk from the queues are sent to node 196. Nodes 191, 193, and 195 specify that statistics are to be collected on messages of priority 1, 2, and 3 respectively that balk from the system. Statistics for all balking messages are collected at node 198. The results for 2 simulations of this modified network can be found in Appendix C.

## 2) Generalized Message Generation

In the original model of the message-switched communication network, it was assumed that the distribution of

Statistics Collection for a QGERT Model of a Four-Node  
Message-Switched Communication Network with Balkers

FIGURE 9.



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message priorities was the same for all combinations of source and destination; and that the distribution of message lengths was a function of the priority level only. In reality, however, the distributions of priority level and message length certainly might vary depending on the source and/or the destination of the message. For example, the distribution of message priority as a function of source and destination may be depicted in the form of a matrix as shown below. The numbers inside the parentheses represent the probabilities of priority 1, priority 2, and priority 3 messages respectively.

		Destination			
		1	2	3	4
Source		1 (.1,.3,.6)	(.2,.3,.5)	(0,.1,.9)	(.2,.2,.6)
2	(0,0,1.0)	(.1,.4,.5)	(.1,.2,.7)	(.1,.3,.6)	
3	(.3,.3,.4)	(.1,.3,.6)	(.1,.4,.5)	(.2,.3,.5)	
4	(0,.2,.8)	(.3,.3,.4)	(.2,.4,.4)	(.1,.3,.6)	

This generalization of the types of messages originating at the various nodes in the network can be incorporated in the QGERT model. First, however, it is necessary to introduce a feature of QGERT that has not yet been described.

QGERT permits the user to access a FORTRAN function within the framework of the symbols that make up the model. The function is given the name USERF. It is written by

the user and may be accessed by either of the following methods at various locations in the model:

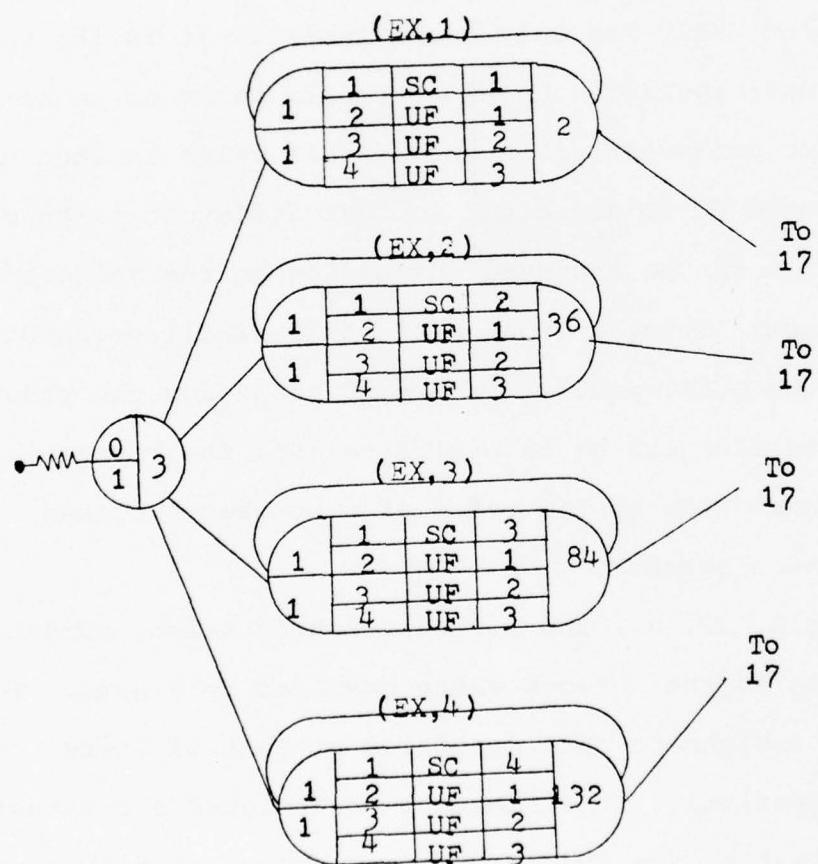
- a) To access the function USERF at a node, the user must specify an attribute assignment with the distribution code UF.
- b) To access the function USERF on an activity, the user must specify an activity time with the distribution code UF.

The function USERF has only one argument. It is the value that the user specifies as an attribute value or an activity time parameter set number. This value is then used in a computed GO TO statement so that different parts of the function can be accessed, depending on the value of the argument. Thus, a great deal of flexibility can be added to the QGERT model. Figure 10 shows how the user-written function can be incorporated into the message generation section of the model of a message-switched communication network.

Nodes 2, 36, 84, and 132 represent the four switching centers in the network where messages originate. Four attribute assignments are specified at each of these nodes respectively. Attribute 1 is assigned a constant value indicating the source of the message. Attributes 2, 3, and 4 specify that function USERF is to be used to assign values for destination, priority level, and message length respectively. Not only is the number of nodes

Message Generation for QGERT Model of a Four-Node  
 Message-Switched Communication Network with  
 FORTRAN Function USERF

FIGURE 10.



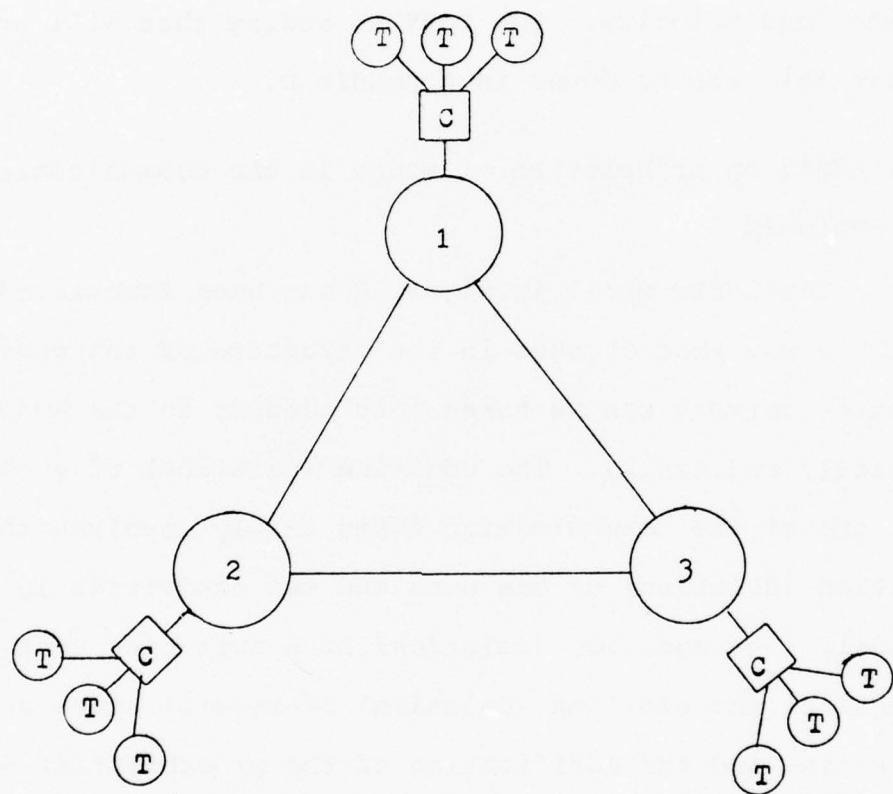
and activities significantly reduced from that of Figure 8, but the origination of messages in the network can be performed in a much more generalized manner. Message priority can be made a function of source and destination; and message length a function of source, destination, and priority. The FORTRAN coding that will accomplish this can be found in Appendix D.

### 3) Addition or Deletion of Nodes in the Communication Network

The QGERT model in Figure 8 has been formulated in such a way that changes in the structure of the communication network can be taken into account in the model quickly and easily. The addition (deletion) of a channel in one of the communication lines simply involves the addition (deletion) of one node and two activities in the model. The addition (deletion) of a switching center requires the addition (deletion) of several nodes and activities and the modification of the probabilities showing the proportions of messages going from the various sources to each of the destinations. To illustrate, suppose switching center number 4 was deleted from the original message-switched network. This would leave the three-node network of Figure 11. Rather than listing the nodes and activities that must be deleted from the model in Figure 8, a revised model of the new three-node network is presented in Figure 12. In general, the

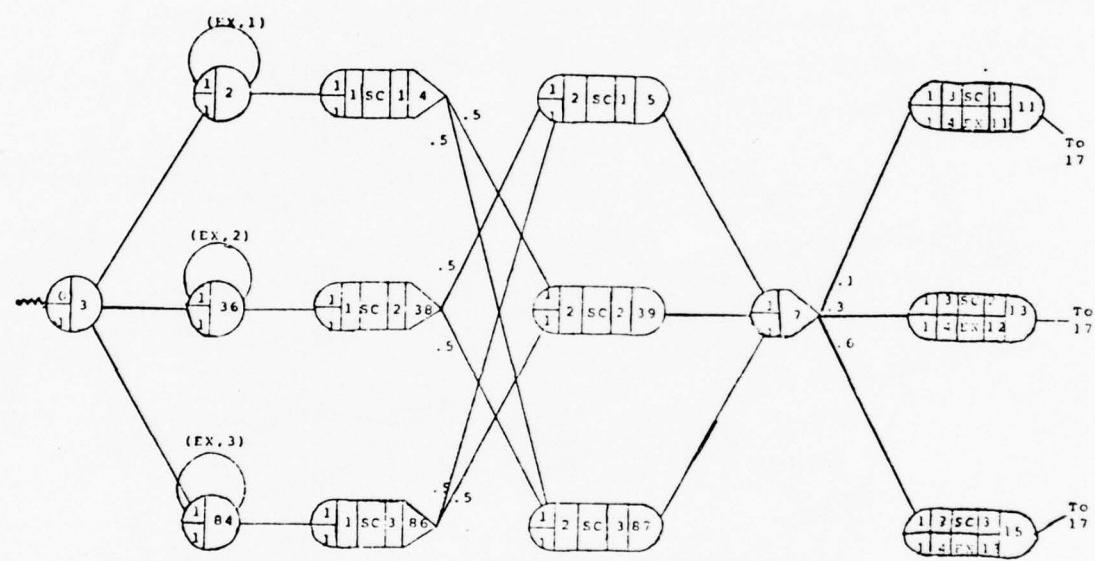
Three-Node Communication Network

FIGURE 11.



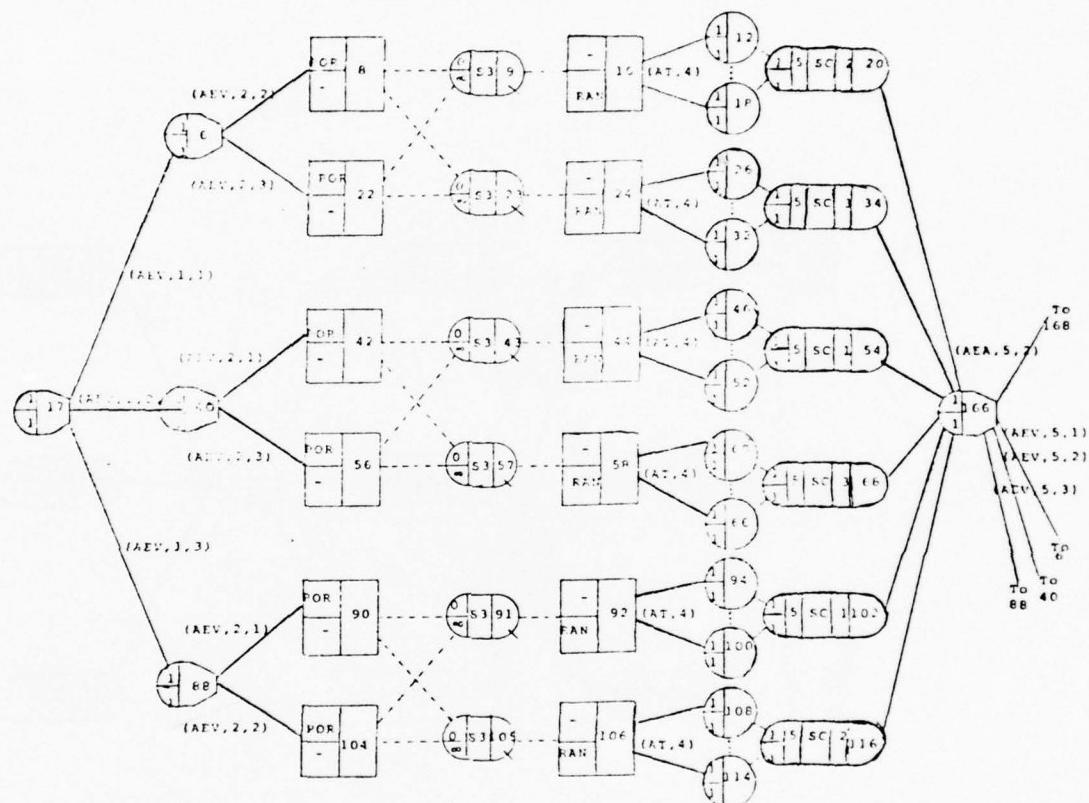
QGERT Model of a Three-Node Message-Switched Communication Network: Message Generation

FIGURE 12(a)



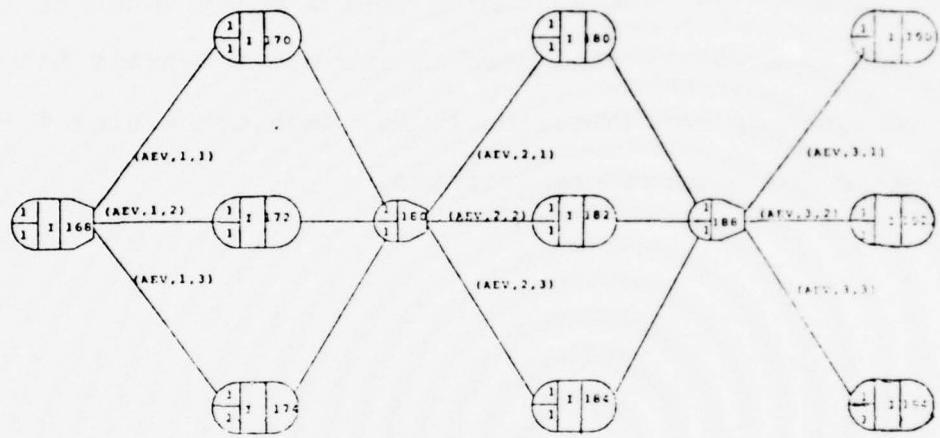
SGAT Model of a Three-Hop Message-Switched  
Communication Network: Routing  
and Transmission

FIGURE 12(b)



QGERT Model of a Three-Node Message-Switched  
Communication Network: Statistics Collection

FIGURE 12(c)



addition (deletion) of a switching center requires the addition (deletion) of approximately 22 nodes in the model and about twice as many activities (the number of activities depending to a slight extent on the total number of switching centers in the network at the time). This assumes that the switching center being added or deleted is directly connected to two other centers in the network by communication lines, each containing 4 channels for message transmission.

MODELLING PACKET-SWITCHED COMMUNICATION  
NETWORKS WITH QGERT

Packet-switching, as discussed in the introduction, is very similar to message-switching. It uses the store-and-forward technique for transmission of messages. The basic difference, however, is that messages are divided into small packets at the source and the packets are transmitted through the network independently. It is quite possible that two packets of the same message might take completely different paths to the specified destination. All packets are of a uniform size. Consequently, processing of packets at the switching centers can be performed very quickly. When all of the packets arrive at the specified destination, they are automatically reassembled into the original message.

The QGERT Model

For the sake of simplicity and to set up a basis for comparison, the four-node communication network of Figure 5 was selected to demonstrate the use of QGERT to model packet-switched networks. The switching centers in the network are now assumed to operate on the principle of packet-switching rather than message-switching. Also, it is assumed that the number of packets in a message is poisson distributed with a mean of 5 packets for

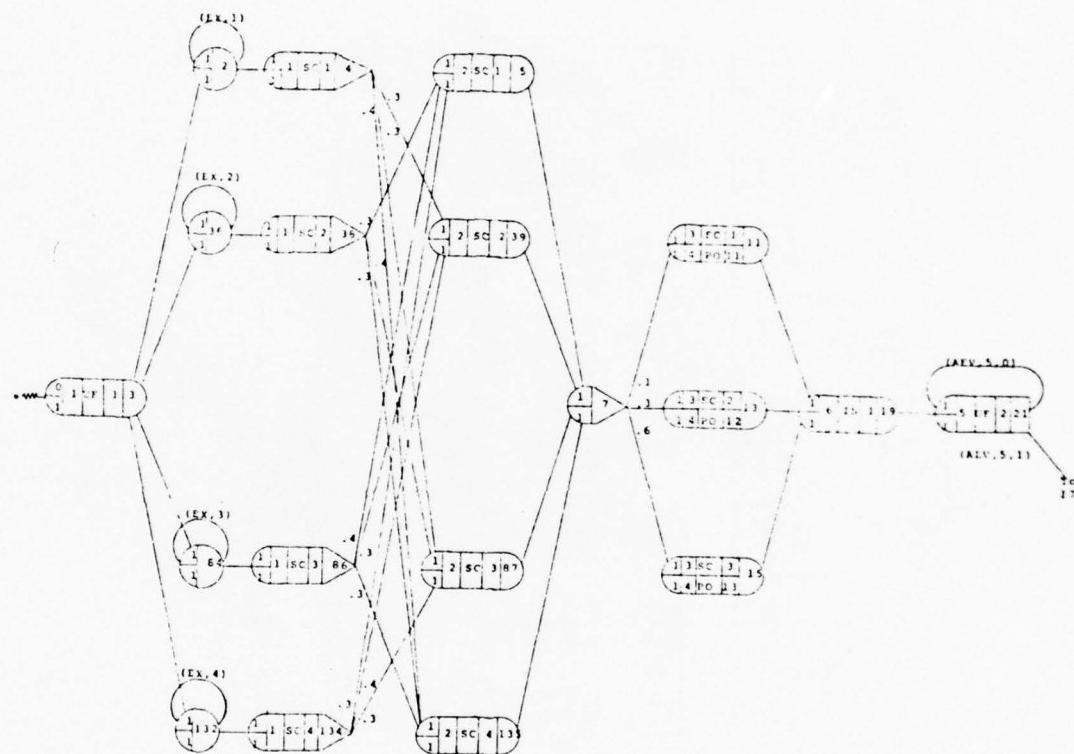
all types of message. Each packet requires 2 time units for transmission. The average variable transmission time per message is therefore 10 time units, which is comparable to the variable transmission time for messages in the message-switched network.

In order to develop a model of a packet-switched network, it is necessary to make use of the user-written FORTRAN function USERF, which was discussed previously. This function is used to separate the messages into packets prior to transmission and to reassemble the packets when transmission is completed. A complete QGERT model of the four-node packet-switched network is presented in Figure 13. Once again, part (a) of the model represents message generation and attribute assignment; part (b) represents routing and transmission of messages; and part (c) represents the collection of statistics reflecting the performance of the network.

Part (a) of Figure 13 is very similar to part (a) of the message-switched model, except for a few minor changes. As in the message-switched model, attributes 3 and 4 are assigned at nodes 11, 13, and 15. Attribute 3 still represents the priority level of the message, but attribute 4 is now assigned a value equal to the number of packets in the message. The distribution code is PO for poisson, with parameter sets 11, 12, and 13 for priority 1, 2, and 3 messages respectively. Following the assignment of

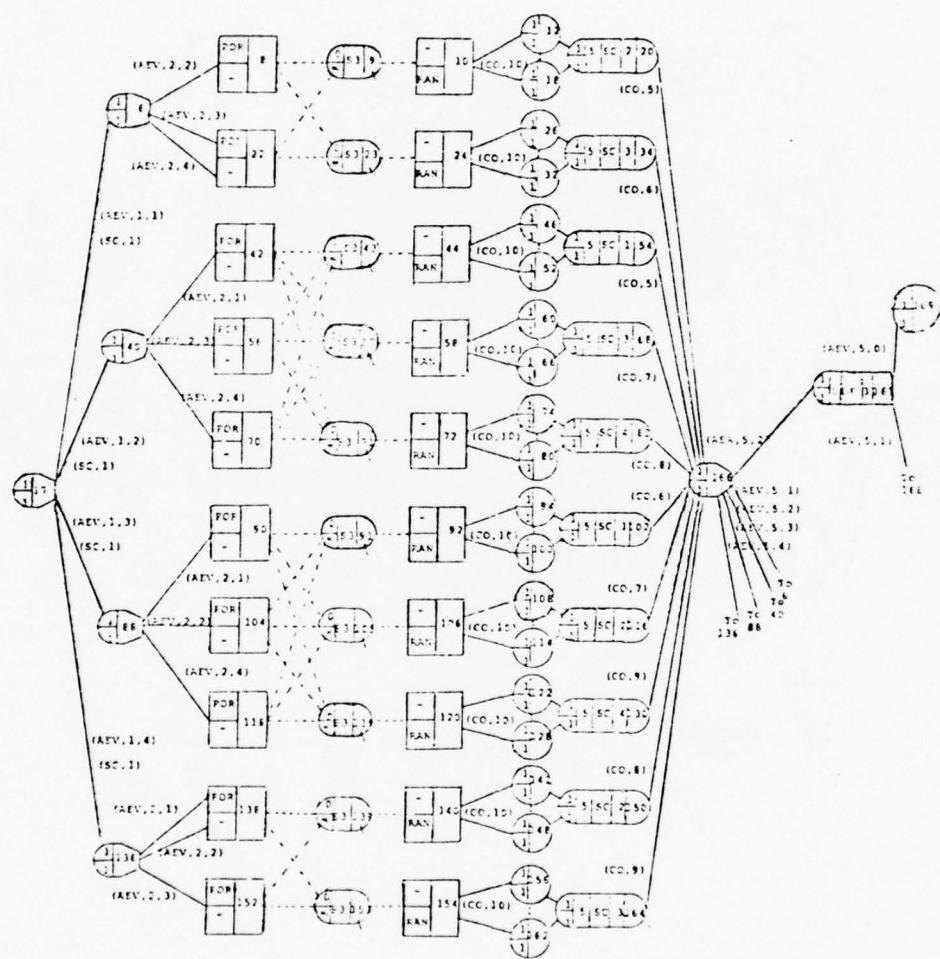
QGERT Model of a Four-Node Packet-Switched  
Communication Network: Message Generation

FIGURE 13(a)

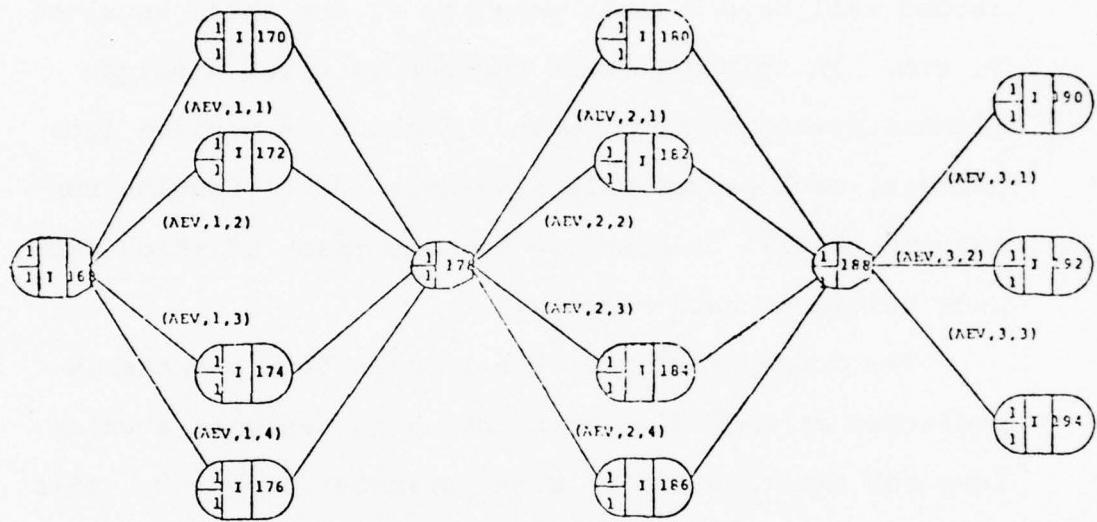


## QGERT Model of a Four-Node Packet-Switched Communication Network: Routing and Transmission

FIGURE 13(b)



QGLRT Model of a Four-Node Packet-Switched Communication Network: Statistics Collection



attributes 3 and 4, all messages are sent to node 19 where a value is assigned from an incremental distribution (IN) beginning with the number 1. This means that the first message will have a value of attribute 6 equal to 1, the second will have a value equal to 2, the third equal to 3, etc. In this way, each message is given a unique identification number. When a message is divided into packets, each packet will have this identification number and it will be possible to keep track of which packets belong to each message.

The decomposition of the message into packets is performed at node 21. Attribute 5 is assigned a value from the distribution UF with parameter number 2. This means that the function USERF will be called with an argument of 2. A listing of the USERF is presented in Figure 14. Initialization of variables is performed first. This occurs at node 3 where USERF is called with an argument of 1. When the number 2 is specified as an argument, packet generation takes place beginning with statement number 20. When a packet is generated, a comparison is made to see if all of the packets in the message have been generated. If they have, a value of 1 is returned for USERF. Otherwise, a value of 0 is returned. The branching from node 21 is conditional-take-first based on this value of USERF. The activity feeding back to node 21 will take place until all of the packets have

ROUTINE Function USERF for the Packet-Switched Model

FIGURE 14.

```

FUNCTION USERF(IFN)
COMMON/TWANS/DESCR(2000),KNOD,MFAD,NODE,NODETH,NODETA(600)
COMMON/PARM/AT:IB(1),ISEED,JTRIB(6),NPMTS,PARAM(100,4),SCALE
COMMON/GENL/IFIN,IFRST,IGRAF,ITRAC,LISTSO,MON,NAME(1?),NORDA,NDAY,
1  NNM,NPINT,NPROJ,NRUN,NRUNS,NSORC(20),NTROS,NTHES,NS_C,NYR,TBEG,
2  TEND
COMMON/USER/MESNUM(40),NPMTS(40),NNMAX,KOUNT
GO TO (10,20,30) IFN
10  NNMAX=40
     KOUNT=0
     DO 1 I=1,NNMAX
        NPMTS(I)=0
        MESNUM(I)=0
1  CONTINUE
     USERF=0.
     RETURN
20  I=JTRIB(6)
     J=DESCR(I+3)
     COUNT=KOUNT+1
     IF(COUNT.EQ.J)GO TO 2
     USERF=0.
     RETURN
2   COUNT=0
     COUNT=0
     USERF=1.
     RETURN
30  K=JTRIB(6)
     ID=DESCR(K+5)
     NTOTAL=DESCR(K+3)
     IF(NTOTAL.NE.1)GO TO 7
     USERF=1.0
     RETURN
7   DO 3 I=1,NNMAX
     IF(MESNUM(I).NE.ID)GO TO 5
3  CONTINUE
     DO 4 J=1,NNMAX
     IF(MESNUM(J).NE.0)GO TO 4
     MESNUM(J)=ID
     NPMTS(J)=1
     USERF=0.
     RETURN
4   CONTINUE
     WRITE(NPINT,100)
100  FORMAT(//,.5K," WARNING - PACKET ASSEMBLY AREA IS FULL.,/")
     DO 300 I=1,NNMAX
     WRITE(NPINT,400)I,MESNUM(I),NPMTS(I)
400  FORMAT(1X,3I10)
     CALL EXIT
5   NPMTS(I)=NPMTS(I)+1
     IF(NPMTS(I).EQ.NTOTAL)GO TO 6
     USERF=0.
     RETURN
6   MESNUM(I)=0
     NPMTS(I)=0
     USERF=1.
     RETURN
END

```

been generated. The individual packets are sent to node 17 and are subsequently treated in the same way as messages in a message-switched system.

The routing and transmission section of the model (Figure 13b) is also very similar to the message-switched model. One of the differences is that the activity time on the service activities is changed to (CO,10). This implies that the transmission time of packets is constant with a value in parameter set number 10. The other change is that nodes 167 and 169 have been added to accommodate the assembly of packets prior to statistics collection. Whenever a packet arrives at node 167, USERF is called with an argument of 3. A check is made to see if it is the last of the packets to arrive for a particular message. The message identification number (attribute 6) is used for this purpose. If it is the last packet, message transmission is complete and the message is sent to node 168 for statistics collection. Otherwise, it is sent to node 169 and is stored until the remainder of the packets arrive. The statistics section of the model is exactly the same as in the message-switched model. Once again, statistics are collected for message transmission times broken down by source, destination, and priority of messages. A complete listing of the Q-GERTS output for the packet-switched network can be found in Appendix E.

### Simulation Results

The results of 1 simulation of the packet-switched network shown in Figure 13 are as follows:

#### 1) Average Message Transmission Time

<u>Message Type</u>	<u>Node No.</u>	<u>No. of Time Units</u>
Priority 1	190	7.7014
Priority 2	192	9.4752
Priority 3	194	20.0360
Source 1	170	22.2323
Source 2	172	9.3886
Source 3	174	10.0729
Source 4	176	19.0693
Destination 1	180	17.8812
Destination 2	182	13.7646
Destination 3	184	12.7050
Destination 4	186	17.9465
All Messages	168	15.2999

#### 2) Average Number in Message Queues

<u>Communication Link</u>	<u>Node No.</u>	<u>Avg. No. in Queue</u>
1 to 2	9	2.1586
1 to 3	23	34.6291
2 to 1	43	5.2832
2 to 3	57	3.1106
2 to 4	71	.8409
3 to 1	91	2.7815
3 to 2	105	2.0000
3 to 4	119	20.2406

4 to 2	139	66.1192
4 to 3	153	1.3979

3) Average Channel Utilization

<u>Communication Link</u>	<u>Activity No.</u>	<u>Percent Busy Time</u>
1 to 2	198	.3400
	197	.3600
	196	.3600
	195	.3600
1 to 3	194	1.0000
	193	1.0000
	192	1.0000
	191	1.0000
2 to 1	190	.8800
	189	.8175
	188	.8461
	187	.8575
2 to 3	186	.5867
	185	.6467
	184	.6667
	183	.6467
2 to 4	182	.3400
	181	.4000
	180	.3400
	179	.3400
3 to 1	178	.4343
	177	.4543
	176	.4343
	175	.4743

3 to 2	174	.5078
	173	.5478
	172	.5000
	171	.5600
3 to 4	170	.9400
	169	.9400
	168	.9521
	167	.9790
4 to 2	166	1.0000
	165	1.0000
	164	1.0000
	163	1.0000
4 to 3	162	.5098
	161	.4898
	160	.5498
	159	.5098

#### Packet-Switching vs. Message Switching

The parameters of the four-node communication network were kept the same for the message-switched and packet-switched models. One of the reasons for this was to be able to make a comparison between the two systems with regards to performance. The average message transmission times for the simulation of the packet-switched network are reprinted in Table 1 along with the results for the message-switched network.

It can be seen that transmission times for the high and middle priority messages were significantly better

for the packet-switched model while the time for the low priority messages was slightly worse. The average time for all messages was approximately 15% less with packet-switching. This is as expected. Because of the pipelining effect, several packets of the same message can be in transmission simultaneously along parallel communication channels. As a result, the transmission times of 7.7014 for priority 1 messages and 9.4752 for priority 2 messages for the packet-switched network are actually less than the expected value of 10 for the sum of the packet transmission times (5 packets per message multiplied by 2 time units per packet).

In both of the models, the transmission times are greatest for the messages that originate at stations 1 and 4 and for those that arrive at these same stations. This is also as anticipated since there is no direct link between the two. The average queue lengths and channel utilization were significantly larger for the packet-switched model because, on the average, five times as many transactions were being placed in the system at any given time.

**Table 1: Comparison of Simulated Message Transmission Times for the Packet-Switched and Message-Switched Model**

Average Transmission Time Units		
<u>Message Type</u>	<u>Packet-Switched</u>	<u>Message-Switched</u>
Priority 1	7.7014	12.3361
Priority 2	9.4752	16.0297
Priority 3	20.0360	19.3908
Source 1	22.2323	27.2049
Source 2	9.3886	12.3500
Source 3	10.0729	14.0068
Source 4	19.0693	17.1912
Destination 1	17.8812	17.4733
Destination 2	13.7646	13.2201
Destination 3	12.7050	15.1907
Destination 4	17.9465	25.4596
All Messages	15.2999	17.7135

## Modelling Circuit-Switched Communication Networks with GASP-IV

An attempt was made to develop QGERT models similar to the ones in the previous two chapters that would accommodate circuit-switched communication networks. The models became so complex and cumbersome, however, that it was determined that QGERT would not be an effective tool for modelling these types of networks. Instead, a GASP-IV model was developed to analyze circuit-switched networks in terms of the measure of effectiveness developed by Podell and described in the introduction of this report.

The model that was developed yields the following statistics for every combination of source, destination, and priority of messages:

1. Calls attempted during the simulation
2. Calls preempted by subscribers of higher priority
3. Calls dropped because of equipment failure
4. Calls blocked by faulty equipment or higher priority calls

GASP-IV can be used for discrete or continuous simulation or a hybrid of the two. This particular model utilizes only the discrete, event-oriented features of GASP-IV. A complete listing of the program can be found in APPENDIX

F. The input to the model consists of parameters describing the network configuration and message traffic characteristics. The format of the input is presented in TABLE 2. The program output consists of an echo check of the input and the statistics described above concerning network performance.

To demonstrate the use of the program, the five-node circuit-switched communication network shown in FIGURE 15 was modelled. The simulation was carried out for a period of 300 time units with statistics being collected for the last 250 time units. The echo check of the input to the program along with a sample of the output can be found in APPENDIX G.

**Five-Node Circuit-Switched Communication Network**

**Figure 15.**

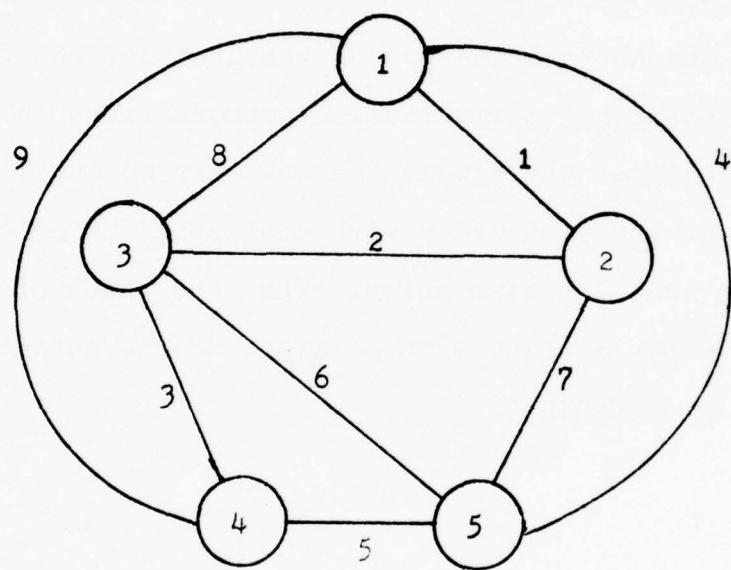


TABLE 2: INPUT FORMAT FOR  
CIRCUIT SWITCHING MOE PROGRAM  
(ALL INPUT RIGHT JUSTIFIED)

CARD 1

Col. 1-5	# of nodes
6-10	# of links
11-18	length of simulation in minutes
19-26	length of initialization run in minutes (50.0 minutes is suggested)

(Cards 2-5 are repeated for each node)

CARD 2

Col. 1-10	Interarrival time between calls in minutes
11-20	Average duration of calls in minutes

CARD 3

Col. 1-5	Probability of priority 1 calls
6-10	" " " 2 "
11-15	" " " 3 "
16-20	" " " 4 "
21-25	" " " 5 "

CARD 4

Col. 1-5	Destination node
5-10	Probability of a call seeking this destination
11-15	Number of alternate routes

CARD 5 (1 card for each route in order of preference)

Col. 1-5	1st link of the route
6-10	2nd link of the route, etc.
:	
:	
36-40	

Return to Card 4 until all destinations are considered.  
Insert a card with a-1 in Cols. 4-5 to mark end of input  
for this node.

Return to Card 2 until input for all nodes has been considered. (Input one card 6 for each link).

CARD 6

Col. 1-5	# of lines in link
6-13	Average time between breakdowns in minutes
14-21	Average duration of breakdown in minutes
22-26	(Nodes connected by
27-31	) the link

Follow these cards by standard GASP IV input cards.

## SUMMARY AND CONCLUSIONS

QGERT was found to be an effective tool for the analysis of performance of store-and-forward communication networks. In particular, once the analyst has become familiar with the QGERT symbol set and related terminology, the ease with which networks can be modelled and modified makes it quite attractive. Compared to a straight simulation, the initial model development stage requires very little time. On the other hand, the time to perform the simulation can become quite large in certain instances. This was particularly true in the case of the packet-switched model, in which a significant amount of time was required to check each packet as it arrived at its destination in the process of reassembling the packets into the original message. Limited computer resources did not permit elaborate experimentation to determine how simulation time increased with the number of nodes in the communication network. A small experiment with three, four, and five node networks, however, seemed to indicate that simulation time would not increase exponentially.

Because the QGERT models can be modified easily, they are well suited to an analysis of alternative network configurations during the design stages of communication network development. For example, the configuration and

message traffic characteristics for the sample four-node network analyzed in this thesis were selected arbitrarily. The results of the simulations indicate that there are severe imbalances and that the network is not well designed to accommodate the existing message traffic. Specifically, the links going from node 1 to node 3, node 2 to node 1, node 3 to node 4, and node 4 to node 2 are characterized by very high channel utilization rates and consequently, very long message queues. The remainder of the links, however, have relatively small utilization rates and message queues. The analyst might want to test whether or not performance of the network could be improved by adding channels to the busy lines and deleting unnecessary channels from the other lines. This can be accomplished within the framework of the QGERT model simply by adding or deleting one node and two activities for each channel. This would mean the addition or deletion of three cards from the input deck.

In the introduction to this report, it was stated that a measure of effectiveness for store-and-forward communication networks should include either estimates of the average message transmission time or the probability that a message is completed within a specified number of time units. The former can be seen directly in the form of the interval statistics collected for each of the models presented in the previous chapters, while the latter can

be determined from the histograms printed as part of the Q-GERTS output. For example, in Appendix C, the histogram for node 190 shows that 29 out of 114 high priority messages had completion times greater than 18 time units. The probability of completing a high priority message in less than 18 time units could therefore be estimated as 75% (85 divided by 114).

It was also stated that the measure of effectiveness should include the probability of balking and the probability of messages being preempted by subscribers of higher precedence. The latter was not included in the models of message-switched and packet-switched networks presented previously, but is discussed in the following section entitled Areas for Further Study. In the message-switched model with limited queue lengths, the output of which can be found in Appendix C, the probability of balking can be estimated from the Q-GERTS summary report. This report shows, for each of the types of messages, the total number that balked and the total number that were completed. The probability of balking can therefore be estimated by dividing the number of balkers by the total number of messages.

QGERT was not found to offer any advantages in the modelling of circuit-switched networks. Instead, a GASP-IV program was developed to estimate performance

measures for networks of this type. The program calculates the various components of the measure of effectiveness formulated by Podell for circuit-switched networks. Simulation time does not grow exponentially as the size of the network increases.

### Areas For Further Study

The QGERT modelling technique has been shown to offer several advantages over other simulation techniques in the modelling of certain types of store-and-forward communication networks. There are a number of things that can still be done, however, to make the modelling effort more efficient and general enough to accommodate any store-and-forward network.

There is, at the time of this writing, an improved version of QGERT being developed. This new version will contain several features which will simplify the modelling of communication networks considerably. For one thing, parallel servers can be modelled with a single activity indicating the number of servers. This means that for each of the communication lines in the network, a single activity can replace the symbol set developed for a communication line in Figure 6. This really becomes significant for lines which contain a large number of communication channels. Another feature offered by the new version is the duplication of similar parts of a QGERT model. This would be very beneficial in the modelling of large communication networks, particularly in the routing and transmission section of the model which is characterized by a series of similar subnetworks

representing the communication lines. Also, a set of subroutines will be available for use in the user functions. The subroutines will permit the addition of much more advanced logic in the models. For example, one of the subroutines can be used to account for preemption of low priority messages in the models of communication networks.

After the new version of QGERT is fully tested and made available for commercial use, it is recommended that the following experiments be carried out:

1. The testing of various routing strategies for messages or packets. This can be accomplished in part by changing the queue selection rules in the S-nodes of the message-switched and packet-switched models. QGERT offers a limited number of such rules. An elaborate strategy might require some modification of the coding in the Q-GERTS program.
2. Experimentation to determine the optimum number of simulations and the length of the simulations in order to establish levels of statistical confidence for the different types of performance measures being investigated in the models.
3. Modelling of existing communication networks such as the packet-switched ARPANET and the message-switched AUTODIN network of the Department of

Defense in order to determine how well the models reflect the actual performance of these networks.

The research described in this paper has taken into consideration message-switched, packet-switched, and circuit-switched communication networks. These are the types of networks that are commonly used in the world today. New networks are currently being developed, however, which represent a hybrid of these three types. In particular, a network might be developed to accommodate voice messages in a circuit-switched manner, with packets of data being transmitted over the communication lines during pauses in the conversation. The ultimate goal of the type of modelling described in this report would be the development of a specialized network technique which would be able to simulate any type of communication network.

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Q-GERTS Output for the Sample Model in FIGURE 4

APPENDIX A

GEERT SIMULATION PROJECT 1 BY J.-J. FABIAN  
DATE 27 1/1977 GEERT VERSION 6/15/75

\*\* NETWORK DESCRIPTION \*\*

NUMBER OF SINK NODES IS 1 NODES (INCLUDING SINKS)  
NUMBER OF NODES TO REALIZE THE NETWORK IS 1  
NUMBER OF SIMULATIONS REQUESTED IS 5  
INITIAL SOURCE NUMBER IS 2345  
NUMBER OF ATTRIBUTES PER TRANSACTION IS 1  
MODIFICATIONS - NO  
DECOMPOSING, FINDING TRACE RUNS - 0, 0  
SCALE FACTOR FOR GC DISTRIBUTION IS 1.0000  
TIME FROM WHICH STATISTICS ARE KEPT .0000  
TYPE OF HIGHLIGHT DESIRED - PLOTTED  
FIRST RUN PRINTOUT OPTION - NO  
LIST ALL INPUT OPTION - YES  
EXECUTION OPTION - E3

\*\* NODE CHARACTERISTICS \*\*

MODE	NUMBER OF REQUIREMENTS	NO. OF SUBSEQUENT REQUIREMENTS	OUTPUT TYPE	MARK	TYPE OF STATISTICS	ATTRIBUTE CRITERION	STATISTICS (CRITERION)	MAINTAIN DESIRED AT RELEASE
2	0	1	0	H		LAST	0	
3	0	1	0	H		LAST	0	
7	1	1	0	H		LAST	0	
8	1	1	0	H		LAST	0	
3	1	1	0	H		LAST	0	
19	0	1	0	H		LAST	0	
11	1	1	0	F		LAST	0	

84

SOURCE NODE NUMBERS  
2 3 10

SINK NODE NUMBERS  
11

STATISTICS COLLECTED ALSO ON NODES  
3 6 7

\*\* QUEUE NODES \*\*

1	2	3	4	5	6	7	8
NODE	INITIAL NO.	MAXIMUM NO.	OUTPUT ALLOWED	PRIORITY SCHEME	MAX BLOCK INCIDENT SERVERS	NODE FOR BALKERS	ASSOCIATED SELECTOR
5	0	3	P	SML ( 1 )	ND	-1	0
6	0	4	P	SML ( 1 )	ND	-1	0

\*\* SELECTOR NODES \*\*

1	2	3	4	5	6	7	8
NODE	SELECTION RULES (QUEUES)	MAX BLOCK INCIDENT SERVERS	NODE FOR BALKERS	ASSOCIATED WITH SELECTOR			
4	SNO	POQ	ND	-1	5	6	

ATTRIBUTE ASSIGNMENT INFORMATION

1	2	3	4	5	6
NODE NUMBER	ATTRIBUTE NUMBER	DISTRIBUTION TYPE	PARAMETER SPECIFICATION		
2	1	SC	1		
3	1	SC	2		

## PARAMETER SPECIFICATION

PARAMETER SET	2-PARAMETERS				4
	1	2	3	4	
1	2.0000	.0000	999.0000	.0000	
2	2.0000	.0000	999.0000	.0000	
3	1.0000	.0000	999.0000	.5000	
4	1.0000	.0000	999.0000	.0000	
5	.0000	.5000	1.5000	.0000	

## \*\* ACTIVITY DESCRIPTION \*\*

1 START TIME	2 END TIME	3 ACTIVITY NAME	4 DURATION TYPE	5 ACTIVITY NAME	6 COUNT TYPE	7 PROBABILITY	8 ADDITIONAL INFORMATION	
							(CODE)	(FILE A) (FILE B) (FILE C)
2	2	BY	1	0	0	1.0000		
3	4	SC	1	0	0	1.0000		
4	3	SC	2	0	0	1.0000		
5	4	SC	1	0	0	1.0000		
6	7	RT	3	192	0	1.0000		
7	7	GT	4	197	0*	1.0000		
8	7	GT	5	196	0*	*5.000		
9	7	SC	6	0	0	*5.000		
10	9	SC	6	0	0	1.0000		
11	11	SC	100	0	0	1.0000		

\*\*\* INPUT CARDS \*\*\*

GEN, J.J.FAGAN, 1,2,1,1977,1,4,1,5,2345,1\*  
SOU, 2,0,1\*  
SOU, 3,0,1\*  
SEL, 4,SNQ,,,,,5,6\*  
QUE, 5,0,3,D,S,1\*  
QUE, 6,0,4,P,S,1\*  
STA, 7,1,1,,B\*  
STA, 8,1,1,,I\*  
STA, 9,1,1,,I\*  
SOU, 10,0,1\*  
SIN, 11,1,1\*  
VAS, 2,1,SC,1\*  
VAS, 3,1,SC,2\*  
PAR, 1,2\*  
PAR, 2,2\*  
PAR, 3,1,,,0.5  
PAR, 4,1\*  
PAR, 5,,0.5,1.5\*  
ACT, 2,2,EX,1\*  
ACT, 2,4,SC,1\*  
ACT, 3,3,EX,2\*  
ACT, 3,4,SC,1\*  
ACT, 5,7,NO,3\*  
ACT, 5,7,CO,4,,,2\*  
ACT, 6,7,UN,5,,,8\*  
ACT, 7,8,,,,,AEV,1,1\*  
ACT, 7,9,,,,,AEV,1,2\*  
ACT, 10,11,SC,100\*  
FIN\*

\*\*\* NO ERRORS DETECTED IN INPUT DATA \*\*\*

\*\*\* EXECUTION WILL BE ATTEMPTED \*\*\*

GERT SIMULATION PROJECT 1 BY J. J. FAGAN  
DATE 2/ 1/ 1977

\*\*FINAL RESULTS FOR 5 SIMULATIONS\*\*

NODE	PROBABILITY	MEAN	STD.DEV.	COEFF. OF VARIANCE	NO OF O.R.S.	MIN.	MAX.	STAT TYPE
11	1.0000	100.0000	.0000	.0000	5.	100.0000	100.0000	F
3	1.0000	2.4078	.5784	.0311	217	477	1.0000	S, 7722
6	1.0300	2.4078	.5784	.0511	717	677	1.0000	I
7	1.0300	1.0329	.0001	.0616	671	671	1.0000	S, 7722

\*\*AVERAGE NUMBER IN Q-NODE\*\*

NO.	MEAN	STD.DEV.	NO. OF OBS.	MIN.	MAX.	MIN.	MAX.
5	.3161	.0461	5.	*2.065	*3731	*	3.
6	.0828	.0326	5.	*0.399	*1162	*	2.

\*\*AVERAGE SERVER UTILIZATION\*\*

SERVER NO.	MEAN	STD.DEV.	NO. OF OBS.	MIN.	MAX.	LONGEST PERIOD TIME	LOCATION
193	.7025	.0277	5.	*6634	*7305	74.0000	12.7045
137	.2554	.0708	5.	*1534	*3117	74.0000	12.7045

\*\*AVERAGE NO. BALKING PER UNIT TIME\*\*

NODE NO.	MEAN	STD.DEV.	NO. OF OBS.	MIN.	MAX.
4	.0000	.0000	5.	*0.000	*0.000

**Q-GERTS Output for the Four-Node Message-Switched  
Network Model in FIGURE 8**

**APPENDIX B**

\*\*FINAL RESULTS FOR 2 SIMULATIONS\*\*

NODE	PROBABILITY	MEAN	STD. DEV.	STDEV. OF MEAN	COEFF. VAR.	NO. OF OBS.	MIN.	MAX.	STAT TYPE
173	1.0000	370.0000	.2000	.0000	2.	300.0000	300.0000	F	
174	1.0000	19.4905	18.3153	.6973	.9445	640.	2.156E	135.6126	I
192	1.0000	16.0707	16.1469	.7731	.9827	335.	2.3507	93.5716	I
193	1.0000	12.3761	6.3270	.7711	.6556	113.	2.1576	33.9095	I
194	1.0000	27.0576	.962074	1.4674	.9510	272.	2.1772	135.6106	I
184	1.0000	15.1902	12.1693	.6950	.8011	305.	2.5167	62.0706	I
192	1.0000	13.2201	10.1549	.6054	.7734	263.	2.1576	64.0573	I
193	1.0000	17.4713	14.0369	.9490	.6033	274.	3.7711	93.5716	I
175	1.0000	17.1912	14.4635	.8364	.8413	299.	2.1576	93.5716	I
174	1.0000	14.0058	9.5850	.5844	.6842	269.	2.5736	52.3529	I
172	1.0000	12.3500	9.7076	.5167	.7051	264.	2.1772	52.6115	I
170	1.0000	27.2049	24.2385	1.4434	.8910	262.	3.5090	135.6106	I
159	1.0000	17.7135	16.5641	.9919	.9351	1134.	2.1576	135.6106	I

\*\*AVERAGE NUMBER IN O-NODE\*\*

NODE	MEAN	STD. DEV.	NO. OF O-N.	MIN.	MAX.
3	0.017	0.017	2*	.0203	0.007
23	1.7117	1.6304	2*	3.3141	4.0292
41	4.064	4.217	2*	1.162	7.745
57	3.955	3.372	2*	1.162	7.745
71	3.010	0.000	2*	0.000	0.023
61	1.652	2.719	2*	0.164	0.000
105	0.047	0.066	2*	0.000	1.001
113	2.1151	1.560	2*	0.100	0.099
139	1.7557	5175	2*	1.5700	2.7406
153	2.059	0.019	2*	2.016	0.019

\*\*NUMBER IN O-NODE\*\*

NODE	MIN.	MAX.
1	*	1.
5	*	14.
6	*	5.
7	*	1.
8	*	1.
9	*	1.
10	*	2.
11	*	1.
12	*	1.
13	*	1.
14	*	1.
15	*	1.

#### **•• AVERAGE SERVER UTILIZATION ••**

••••• TIME PERIODS AND SEQUENCES

MEAN	STD. DEV.	NO. OF OBS.	MAX.	LONGEST PERIOD TIDE	
				PERIOD	LAST
1.129	.2600	2*	.2967	.2714	.2714
1.127	.3745	2*	.3163	.3130	.3130
1.126	.0542	2*	.2364	.6797	.6797
1.125	.1590	2*	.2111	.5711	.5711
1.124	.3774	2*	.0025	.9300	.9300
1.123	.6755	2*	.1718	.8720	.8720
1.122	.0667	2*	.0622	.2014	.2014
1.121	.9159	2*	.3611	.6521	.6521
1.120	.3611	2*	.6058	.6141	.6141
1.119	.6055	2*	.1569	.6146	.6146
1.118	.2711	2*	.1305	.5412	.5412
1.117	.6643	2*	.3765	.5794	.5794
1.116	.7113	2*	.1090	.5051	.5051
1.115	.6594	2*	.1037	.3049	.3049
1.114	.5523	2*	.0630	.6107	.6107
1.113	.4610	2*	.0034	.4106	.4106
1.112	.6115	2*	.5725	.6103	.6103
1.111	.3221	2*	.1510	.5127	.5127
1.110	.6133	2*	.1721	.2306	.2306
1.109	.2254	2*	.0249	.2122	.2122
1.108	.8109	2*	.1293	.2612	.2612
1.107	.3133	2*	.2720	.3090	.3090
1.106	.4717	2*	.3787	.4050	.4050
1.105	.4671	2*	.1276	.4161	.4161
1.104	.1753	2*	.0171	.3455	.3455
1.103	.6121	2*	.0119	.5217	.5217
1.102	.5530	2*	.1300	.4671	.4671
1.101	.2547	2*	.2457	.5771	.5771
1.100	.1725	2*	.1697	.4025	.4025
1.099	.4700	2*	.2524	.2256	.2256
1.098	.1729	2*	.0361	.5551	.5551
1.097	.7711	2*	.0550	.5273	.5273
1.096	.2711	2*	.0104	.6110	.6110
1.095	.6115	2*	.0157	.7576	.7576
1.094	.7487	2*	.0169	.8704	.8704
1.093	.6117	2*	.0772	.8022	.8022
1.092	.5567	2*	.1722	.7559	.7559
1.091	.4227	2*	.0677	.6051	.6051
1.090	.4255	2*	.0677	.7003	.7003
1.089	.4227	2*	.0577	.8132	.8132
1.088	.4255	2*	.0303	.3729	.3729
1.087	.4227	2*	.1134	.3525	.3525
1.086	.4255	2*	.0677	.4462	.4462
1.085	.4227	2*	.0677	.3501	.3501
1.084	.4255	2*	.0677	.4775	.4775

Q-GERTS Output for the Message-Switched Model  
with Balkings

APPENDIX C

AD-A041 314

LEHIGH UNIV BETHLEHEM PA DEPT OF INDUSTRIAL ENGINEERING F/G 17/2  
EXTENSIONS OF STOCHASTIC NETWORK THEORY TO FACILITATE THE DEVEL--ETC(U)  
1977 G E WHITEHOUSE, J J FAGAN N00014-76-C-0900

UNCLASSIFIED

IE-77-OR-1

NL

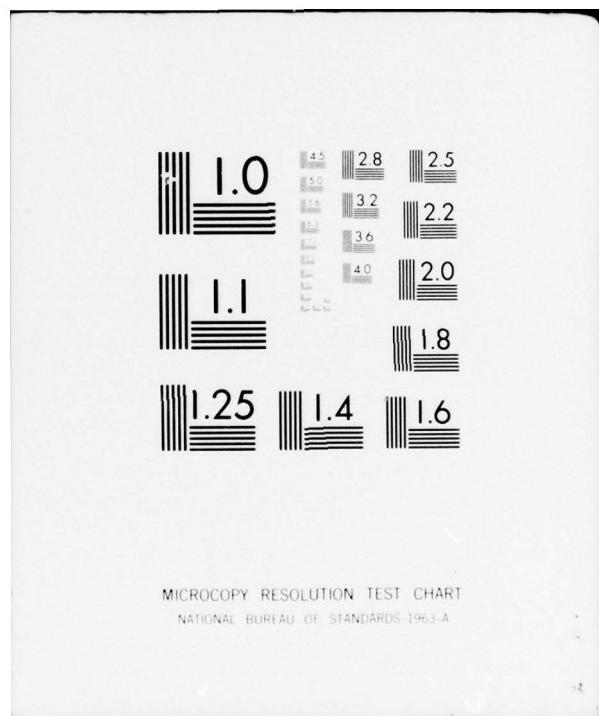
2 OF 2

AD  
A041314



END

DATE  
FILMED  
7-77



CERT SIMULATION PROJECT 2 BY J.J. FAGAN  
DATE 2/15/1977

\*\*FINAL RESULTS FOR 2 SIMULATIONS\*\*

CODE	PROBABILITY	M-EAN	STD. DEV.	CFR M-EAN	CDFFF*	NO OF OUTS	MIN.	MAX.	STAT TYPE
17.3	1.0000	220.0000	.0003	.0003	*.0003	2.	300.0000	300.0000	F
2.34	1.0000	2.7273	.66204	*.8169	1.7066	32.	1.0350	18.5215	I
1.75	1.0000	2.7072	.55311	1.0510	1.6413	13.	1.3760	17.6045	I
19.2	1.0000	3.5331	.62225	2.5031	1.6905	7.	1.2000	1A.5215	I
19.1	1.0000	3.5131	1.2564	*.5131	*.8306	6.	1.3000	4.0287	I
10.4	1.0000	12.1150	13.6880	.5222	*.7938	687.	2.1626	96.9495	I
17.7	1.0000	14.9537	11.0990	.6239	*.7526	328.	2.2360	31.6762	I
1.10	1.0000	14.7561	11.5312	1.0800	*.7435	114.	2.1241	67.2738	I
1.16	1.0000	14.6276	15.1713	*.9132	*.8263	276.	2.3321	96.9495	I
15%	1.0000	14.9575	11.3885	.6916	*.7616	271.	2.5551	64.6007	I
1.92	1.0000	12.4971	10.5559	.6263	*.8431	283.	2.1241	62.6251	I
1.43	1.0000	15.6011	12.8555	.7423	*.6900	299.	4.0873	67.2733	I
1.76	1.0000	16.0461	12.9576	.7887	*.8079	270.	2.1241	67.2738	I
17.4	1.0000	15.3076	10.8892	.6316	*.7255	297.	3.4012	51.5445	I
1.72	1.0000	13.6780	10.9319	.6521	*.7997	201.	2.3321	66.6603	I
17.0	1.0000	20.3393	15.3356	.9149	*.7540	281.	3.5206	99.9495	I
10.8	1.0000	16.2489	12.8625	.3828	*.7916	1129.	2.1241	96.9495	I

\*\*ENVIRONMENTAL HAZARD IN C-HOUSE\*\*

NAME	PLAN	STD. DEV.	NO OF OUTS	MIN.	MAX.	MIN.	MAX.
N-1	-.0214	.0113	2.	*.0155	*.0250	1.	1.
2A1	1.0464	.2729	2.	1.4510	1.6359	1.	1.
A2	-4.6184	.1790	2.	*.3466	*.5810	5.	5.
B2	-1.1707	.3175	2.	*.1075	*.1233	2.	2.
71	*.0716	.1015	2.	*.0010	*.1166	2.	2.
91	*.5510	.0559	2.	*.5115	*.5915	5.	5.
105	*.0615	*.0622	2.	*.0010	*.0011	1.	1.
119	*.5412	*.5992	2.	*.5129	*.6532	5.	5.
123	*.5163	*.6317	2.	*.0596	*.0510	4.	4.
163	*.0149	.0234	2.	*.0004	*.0314	1.	1.

\*\*NUMBER IN Q-HOUSE\*\*

\*\*TIME PERIODS OF STEPS\*\*

\*\*AVERAGE SEVER UTILIZATION\*\*

Score	Mean	Std. Dev.	No. of Obs.	Min.	Max.	Logistic Period	Logistic Longest Period
100	4.075	1.046	21	4.208	5.745	26.442	72.561
101	4.228	1.217	21	5.710	6.827	46.841	65.437
102	4.272	1.026	21	2.772	4.222	40.710	33.676
103	4.327	1.041	21	1.593	3.359	57.742	23.324
104	4.641	1.459	21	6.956	9.73	13.142	86.677
105	4.810	1.060	21	8.056	9.204	12.163	46.302
106	4.964	1.471	21	7.137	9.244	15.124	66.652
107	5.122	1.692	21	7.634	9.216	12.501	47.241
108	5.171	1.145	21	6.035	8.075	27.613	41.229
109	5.476	0.507	21	6.822	7.663	29.334	41.394
110	5.527	1.876	21	5.018	7.663	29.334	41.394
111	5.670	1.270	21	6.702	8.075	27.613	41.229
112	5.840	1.274	21	6.178	7.663	27.613	41.229
113	5.954	1.745	21	5.277	7.726	19.395	46.637
114	6.050	1.327	21	6.210	8.611	12.137	51.655
115	6.123	1.310	21	5.344	7.295	32.336	41.017
116	6.174	0.676	21	5.018	8.075	30.608	46.420
117	6.184	1.275	21	6.677	8.736	16.204	41.762
118	6.215	1.145	21	6.717	8.736	16.204	41.762
119	6.270	1.876	21	5.018	7.663	27.613	41.229
120	6.357	1.274	21	6.211	8.075	27.613	41.229
121	6.460	1.274	21	6.362	8.075	31.875	46.637
122	6.544	1.745	21	5.018	8.075	27.613	41.229
123	6.606	1.327	21	6.210	8.611	20.591	46.420
124	6.651	1.275	21	6.233	8.327	35.112	46.787
125	6.710	0.676	21	5.730	7.110	22.325	42.917
126	6.710	1.145	21	6.625	7.022	22.921	61.356
127	6.759	0.637	21	6.625	7.022	22.921	61.356
128	6.875	1.274	21	6.071	6.604	27.613	51.431
129	6.975	1.274	21	6.277	6.603	52.333	22.290
130	7.006	1.745	21	6.270	8.276	60.032	31.875
131	7.082	1.275	21	6.153	7.172	67.957	20.591
132	7.170	0.676	21	6.233	8.327	35.112	46.787
133	7.616	1.145	21	6.625	7.022	22.921	61.356
134	7.676	1.274	21	6.625	7.022	22.921	61.356
135	7.752	0.637	21	6.625	7.022	22.921	61.356
136	7.875	1.274	21	6.071	6.604	27.613	51.431
137	7.956	1.274	21	6.277	6.603	52.333	22.290
138	8.006	1.745	21	6.270	8.276	60.032	31.875
139	8.082	1.275	21	6.153	7.172	67.957	20.591
140	8.170	0.676	21	6.233	8.327	35.112	46.787
141	8.510	1.145	21	6.625	7.022	22.921	61.356
142	8.510	1.274	21	6.625	7.022	22.921	61.356
143	8.592	0.637	21	6.625	7.022	22.921	61.356
144	8.676	1.274	21	6.071	6.604	27.613	51.431
145	8.752	0.637	21	6.277	6.603	52.333	22.290
146	8.875	1.274	21	6.270	8.276	60.032	31.875
147	8.956	1.274	21	6.153	7.172	67.957	20.591
148	9.044	1.745	21	6.231	8.327	35.112	46.787
149	9.140	1.275	21	6.210	8.611	20.591	46.420
150	9.583	0.637	21	6.917	7.453	16.431	45.235
151	9.663	1.145	21	7.763	8.736	19.723	51.431
152	9.752	1.274	21	6.627	7.110	22.325	61.356
153	9.837	0.637	21	6.717	7.663	27.613	41.229
154	9.910	1.274	21	6.071	6.604	27.613	41.229
155	9.992	0.637	21	6.277	6.603	52.333	22.290
156	10.075	1.274	21	6.270	8.276	60.032	31.875
157	10.156	0.637	21	6.153	7.172	67.957	20.591
158	10.237	1.274	21	6.231	8.327	35.112	46.787
159	10.317	0.637	21	6.210	8.611	20.591	46.420
160	10.396	1.274	21	6.704	7.663	27.613	41.229
161	10.476	0.637	21	7.014	7.663	50.668	33.224
162	10.556	1.145	21	3.187	6.760	45.704	27.791
163	10.636	1.274	21	3.207	6.126	60.032	27.075

\*\*AVG. NO. WALKING PER UNIT TIME\*\*

Score	Mean	Std. Dev.	No. of Units	Min.	Max.
100	4.075	0.700	21	-0.030	-0.000
101	4.228	0.700	21	-0.030	-0.000
102	4.272	0.700	21	-0.030	-0.000
103	4.313	0.700	21	-0.030	-0.000
104	4.313	0.700	21	-0.030	-0.000
105	4.313	0.700	21	-0.030	-0.000
106	4.313	0.700	21	-0.030	-0.000
107	4.313	0.700	21	-0.030	-0.000
108	4.313	0.700	21	-0.030	-0.000
109	4.313	0.700	21	-0.030	-0.000
110	4.313	0.700	21	-0.030	-0.000
111	4.313	0.700	21	-0.030	-0.000
112	4.313	0.700	21	-0.030	-0.000
113	4.313	0.700	21	-0.030	-0.000
114	4.313	0.700	21	-0.030	-0.000
115	4.313	0.700	21	-0.030	-0.000
116	4.313	0.700	21	-0.030	-0.000
117	4.313	0.700	21	-0.030	-0.000
118	4.313	0.700	21	-0.030	-0.000
119	4.313	0.700	21	-0.030	-0.000
120	4.313	0.700	21	-0.030	-0.000
121	4.313	0.700	21	-0.030	-0.000
122	4.313	0.700	21	-0.030	-0.000
123	4.313	0.700	21	-0.030	-0.000
124	4.313	0.700	21	-0.030	-0.000
125	4.313	0.700	21	-0.030	-0.000
126	4.313	0.700	21	-0.030	-0.000
127	4.313	0.700	21	-0.030	-0.000
128	4.313	0.700	21	-0.030	-0.000
129	4.313	0.700	21	-0.030	-0.000
130	4.313	0.700	21	-0.030	-0.000
131	4.313	0.700	21	-0.030	-0.000
132	4.313	0.700	21	-0.030	-0.000
133	4.313	0.700	21	-0.030	-0.000
134	4.313	0.700	21	-0.030	-0.000
135	4.313	0.700	21	-0.030	-0.000
136	4.313	0.700	21	-0.030	-0.000
137	4.313	0.700	21	-0.030	-0.000
138	4.313	0.700	21	-0.030	-0.000
139	4.313	0.700	21	-0.030	-0.000
140	4.313	0.700	21	-0.030	-0.000
141	4.313	0.700	21	-0.030	-0.000
142	4.313	0.700	21	-0.030	-0.000
143	4.313	0.700	21	-0.030	-0.000
144	4.313	0.700	21	-0.030	-0.000
145	4.313	0.700	21	-0.030	-0.000
146	4.313	0.700	21	-0.030	-0.000
147	4.313	0.700	21	-0.030	-0.000
148	4.313	0.700	21	-0.030	-0.000
149	4.313	0.700	21	-0.030	-0.000
150	4.313	0.700	21	-0.030	-0.000
151	4.313	0.700	21	-0.030	-0.000
152	4.313	0.700	21	-0.030	-0.000
153	4.313	0.700	21	-0.030	-0.000
154	4.313	0.700	21	-0.030	-0.000
155	4.313	0.700	21	-0.030	-0.000
156	4.313	0.700	21	-0.030	-0.000
157	4.313	0.700	21	-0.030	-0.000
158	4.313	0.700	21	-0.030	-0.000
159	4.313	0.700	21	-0.030	-0.000
160	4.313	0.700	21	-0.030	-0.000
161	4.313	0.700	21	-0.030	-0.000
162	4.313	0.700	21	-0.030	-0.000
163	4.313	0.700	21	-0.030	-0.000
164	4.313	0.700	21	-0.030	-0.000
165	4.313	0.700	21	-0.030	-0.000
166	4.313	0.700	21	-0.030	-0.000
167	4.313	0.700	21	-0.030	-0.000
168	4.313	0.700	21	-0.030	-0.000
169	4.313	0.700	21	-0.030	-0.000
170	4.313	0.700	21	-0.030	-0.000
171	4.313	0.700	21	-0.030	-0.000
172	4.313	0.700	21	-0.030	-0.000
173	4.313	0.700	21	-0.030	-0.000
174	4.313	0.700	21	-0.030	-0.000
175	4.313	0.700	21	-0.030	-0.000
176	4.313	0.700	21	-0.030	-0.000
177	4.313	0.700	21	-0.030	-0.000
178	4.313	0.700	21	-0.030	-0.000
179	4.313	0.700	21	-0.030	-0.000
180	4.313	0.700	21	-0.030	-0.000
181	4.313	0.700	21	-0.030	-0.000
182	4.313	0.700	21	-0.030	-0.000
183	4.313	0.700	21	-0.030	-0.000
184	4.313	0.700	21	-0.030	-0.000
185	4.313	0.700	21	-0.030	-0.000
186	4.313	0.700	21	-0.030	-0.000
187	4.313	0.700	21	-0.030	-0.000
188	4.313	0.700	21	-0.030	-0.000
189	4.313	0.700	21	-0.030	-0.000
190	4.313	0.700	21	-0.030	-0.000
191	4.313	0.700	2		

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**FORTRAN Function USERF for the Message-Switched Model  
with Generalized Message Generation**

**APPENDIX D**

```

FUNCTION USERF(IFN)
DIMENSION PDES(4,4),PPRI(4,3),TIME(4,3)
COMMON/PARM/AIRIB(1),ISEED,JTR10(6),NPRMS,PARAM(100,4),SCALE
DATA((PDES(I,J),J=1,4),I=1,4)/0.,.3,.3,.4,.3,0.,.4,.3,.4,.3,0.,.3,
1 .3,.4,.3,0./
DATA((PPRI(I,J),J=1,3),I=1,4)/.1,.3,.6,.1,.4,.5,.2,.3,.5,.1,.2,.7/
DATA((TIME(I,J),J=1,3),I=1,4)/5.,7.,10.,6.,8.,10.,8.,9.,12.,5.,
1 8.,10./
NSOU=JTRIB(1)
RN=DRAND(ISEED)
CUMPROB=0.
GO TO(1,2,3)IFN
1 DO 10 J=1,4
IF(NSOU.EQ.J)GO 10 10
CUMPROB=CUMPROB+PDES(NSOU,J)
IF(RN.LT.CUMPROB)GO TO 11
10 CONTINUE
11 IDES=J
USERF=IDES
RETURN
2 DO 20 J=1,3
CUMPROB=CUMPROB+PPRI(NSOU,J)
IF(RN.LT.CUMPROB)GO TO 21
20 CONTINUE
21 IPRI=J
USERF=IPRI
RETURN
3 USERF=-TIME(IDES,IPRI)* ALOG(RN)
RETURN
END

```

Q-GERTS Output for the Four-Node Packet-Switched  
Network Model in FIGURE 13

APPENDIX E

GERT SIMULATION PROJECT 3 BY J.J. FAGAN  
DATE 3/ 1/ 1977

\*\*FINAL RESULTS FOR 1 SIMULATION\*\*

NODE	PROBABILITY	MEAN	STD.DEV.	STD.DEV. OF MEAN	CORR. VAR.	NO OF OBS.	MIN.	MAX.	STAT TYPE
173	1.0000	150.0000	.0000	.0000	.0000	1.	150.0000	150.0000	F
174	1.0000	20.0160	17.7111	1.4608	.0142	147*	4.0100	71.7300	I
192	1.0000	9.4752	6.1355	.4539	.4364	93*	4.0200	25.4713	I
120	1.0000	7.7014	2.1595	.4091	.2604	79*	4.0100	16.0168	I
146	1.0000	17.9465	16.0248	2.0074	.8957	64*	4.0000	71.2727	I
154	1.0000	12.7050	10.5073	1.2238	.8270	73*	4.5103	52.3942	I
192	1.0000	13.7646	13.5055	1.6394	1.0030	71*	6.7550	52.3370	I
180	1.0000	17.6812	16.0963	2.5592	1.0120	50*	5.5000	71.7300	I
176	1.0000	19.0693	19.5947	2.3425	1.0279	70*	4.5200	71.7300	I
174	1.0000	19.0729	5.7829	.7728	.5741	56*	4.0100	31.1467	I
174	1.0000	9.7996	4.8226	.5016	.5137	60*	4.0000	51.0295	I
173	1.0000	22.2323	16.6406	2.0965	.7435	63*	5.0000	71.2727	I
153	1.0000	15.2999	16.6364	.9112	.9566	253*	4.0100	71.7300	I

\*\*AVERAGE NUMBER IN Q-NODE\*\*

NODE	MEAN	STD.DEV.	NO OF OBS.	MIN.	MAX.	MIN.	MAX.
9	2.1576	.0000	1*	2.1576	2.1576	*	15*
23	36.6231	.0000	1*	36.6231	36.6231	1*	43*
43	5.2012	.0010	1*	5.2012	5.2012	*	26*
57	3.1135	.0001	1*	3.1135	3.1135	*	19*
71	4.6339	.0003	1*	4.6339	4.6339	*	10*
91	2.7915	.0000	1*	2.7915	2.7915	*	22*
105	2.0000	.0003	1*	2.0000	2.0000	*	12*
119	20.2406	.0000	1*	20.2406	20.2406	*	53*
139	65.1192	.0000	1*	65.1192	65.1192	1*	89*
153	1.3979	.0000	1*	1.3979	1.3979	*	11*

\*\*AVERAGE SERVER UTILIZATION\*\*

SERVER NO.	MEAN	STD. DEV.	NO. OF OBS.	MIN.	MAX.	LONGEST PERIOD IDLE	LONGEST PERIOD BUSY
198	.3400	.0000	11	.3400	.3400	34.4403	22.0000
197	.3630	.0000	11	.3600	.3600	34.4403	24.0000
195	.3500	.0000	11	.3500	.3500	34.4403	24.0000
195	.3503	.0000	11	.3500	.3500	34.4403	24.0000
196	.3603	.0000	11	.3600	.3600	34.4403	24.0000
196	.3700	.0000	11	.3700	.3700	34.4403	24.0000
193	.3000	.0000	11	.3000	.3000	100.0000	100.0000
193	.3000	.0000	11	.3000	.3000	100.0000	100.0000
192	1.0003	.3000	11	1.0000	1.0000	100.0000	100.0000
191	1.0300	.0000	11	1.0000	1.0000	100.0000	100.0000
190	.8300	.0000	11	.8000	.8000	21.0754	21.0754
189	.8175	.0000	11	.8175	.8175	21.5007	21.5007
189	.8461	.0000	11	.8461	.8461	6.6503	6.6503
187	.4575	.0000	11	.4575	.4575	29.6007	29.6007
185	.5957	.0000	11	.5957	.5957	6.6503	6.6503
185	.6457	.0000	11	.6467	.6467	14.7645	14.7645
154	.6667	.0000	11	.6667	.6667	9.4147	14.7645
183	.5467	.0000	11	.5467	.5467	6.9238	16.0000
182	.3403	.0000	11	.3403	.3403	6.1238	14.7575
191	.4000	.0000	11	.4000	.4000	12.0092	6.5000
180	.3400	.0000	11	.3400	.3400	10.5692	2.0000
179	.3100	.0000	11	.3100	.3100	12.0892	8.0000
178	.4363	.0000	11	.4343	.4343	14.6127	14.6127
177	.4543	.0000	11	.4543	.4543	12.0000	12.0000
176	.4143	.0000	11	.4143	.4143	16.6127	14.0000
175	.4743	.0000	11	.4743	.4743	15.6127	14.5917
174	.5078	.0000	11	.5078	.5078	16.5003	16.5049
173	.5478	.0000	11	.5478	.5478	14.0175	14.0175
172	.5000	.0000	11	.5000	.5000	15.5717	15.5717
171	.5600	.0000	11	.5600	.5600	14.5349	14.5349
170	.9400	.0000	11	.9400	.9400	4.5729	7.8.7423
169	.9400	.0000	11	.9400	.9400	4.5729	7.8.7423
169	.9521	.0000	11	.9521	.9521	2.6506	7.4.0531
167	.9793	.0000	11	.9790	.9790	1.4201	7.4.7513
166	1.0000	.0000	11	1.0000	1.0000	.0000	100.0000
165	1.0000	.0000	11	1.0000	1.0000	.0000	100.0000
164	1.0000	.0000	11	1.0000	1.0000	.0000	100.0000
163	1.0000	.0000	11	1.0000	1.0000	.0000	100.0000
162	.5098	.0000	11	.5098	.5098	1.0120	8.0000
161	.4998	.0000	11	.4998	.4998	10.0313	12.0000
160	.5498	.0000	11	.5498	.5498	6.0120	12.0000
159	.5098	.0000	11	.5098	.5098	6.0920	12.0000

LOGIC NODE	CELL MIDPOINT	FREQUENCIES															
		0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
273	.00	1.00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
414	.00	1.00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
152	.00	1.00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
170	.00	1.00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
168	.00	1.10	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
164	.00	1.00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
162	.00	1.00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
140	.00	1.00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
176	.00	1.00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
174	.00	1.00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
172	.00	1.00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
170	.00	1.00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
168	.00	1.00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
23	.00	1.00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
71	.00	1.00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
91	.00	1.00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

**Listing of GASP-IV Program for Circuit-Switched  
Communication Networks**

**APPENDIX F**

```

PROGRAM MAIN(INPUT,OUTPUT,TAPE5=INPUT,TAPE6=OUTPUT)
DIMENSION NSET(10000)
COMMON/QSET/(10000)
1 NCODR, NNAPO, NNAPT, NNATR, NNFILE, NNQ(100), NNTRY, NPPRT, PPAPM(50,4),
2 TNOW, TTBEGL, TTCLR, TTIN, TTRIB(25), TTSET
COMMON/UDOWN/IRT( 500,8),MLK(100),NLK(100),LST(100),TBB(100),
1 TOB(100),PLACE(15,15),CARR(15),COUR(15),PRI(15,5),ICA(15,15,5),
2 ICR(15,15,5),ICP(15,15,5),ICD(15,15,5),ICC(15,15,5),
3 IIR(15,15,8),ITEMP(8),NODES,NLINK,ZENGT,STRST
EQUIVALENCE(NSET(1),QSET(1))
NCDR=5
NPNT=6
READ(NCDR,1)NODES,NLINK,ZENGT,STRST
1 FORMAT(1Z15,2F8.0)
DO 11 IZM=1,NODES
DO 11 IZN=1,NODES
11 PLACE(IZM,IZN)=0
IZZ=1
C INITIALIZE ROUTE FILE
DO 2 I=1,500
DO 2 J=1,8
2 IRT(I,J)=0
DO 3 I=1,NODES
DO 3 J=1,NODES
DO 3 K=1,8
3 IIRT(I,J,K)=0
C INPUT INFORMATION ABOUT SOURCES
WRITE(NPNT,4)
4 FORMAT(1BX,20HFCHECK FOR NODES)
DO 5 II=1,NODES
PEAJ(NCDR,7)CARR(II),COUR(II)
5 FORMAT(2F10.5)
WRITE(NPNT,8)II,CARR(II),COUR(II)
8 FORMAT(//,10X,13HCALLS FROM SOURCE ,I2,//,15X,
1 27HAVERAGE TIME BETWEEN CALLS ,F10.5,/,15X,
2 25HAVERAGE DURATION OF CALL ,F10.5)
C PRIORITY OF CALLS
READ(NCDR,9)PRI(II,K),K=1,5
9 FORMAT(5F5.3)
WRITE(NPNT,10)(PRI(II,K),K=1,5)

10 FORMAT(//,15X,35HPROBABILITY OF PRIORITY 1 CALLS IS ,F5.3,/,
1 15X,35HPROBABILITY OF PRIORITY 2 CALLS IS ,F5.3,/,
2 15X,35HPROBABILITY OF PRIORITY 3 CALLS IS ,F5.3,/,
3 15X,35HPROBABILITY OF PRIORITY 4 CALLS IS ,F5.3,/,
4 15X,35HPROBABILITY OF PRIORITY 5 CALLS IS ,F5.3)
C DESTINATION INFORMATION
15 READ(NCDR,12)JJ,PROB,NUM
IF(JJ.LT.0)GO TO 5
WRITE(NPNT,13)JJ,PROB
12 FORMAT(15,F5.3,I5)
13 FORMAT(//,1BX,36HPROBABILITY OF A CALL GOING TO SINK ,I5,4H IS ,
1 F5.3/,24X,30HEOUTES IN ORDER OF PREFERENCE )
1 PLACE(1,JJ)=PROB
DO 17 I=1,NUM
PEAJ(NCDR,19)(ITEMP(J),J=1,8)
19 FORMAT(8I5)
IE=?
24 IF(ITEMP(IE).EQ.0)GO TO 25
IE=IE+1
IF(IE.EQ.9)GO TO 25
GO TO 24
25 IF=IE-1
DO 26 J=1,IE
IRT(IZZ,J)=ITEMP(J)
IIRT(11,JJ,IE)=IZZ
IZZ=IZZ+1
GO TO (31,32,33,34,35,36,37,38) IE
31 WRITE(NPNT,39)ITEMP(1)
GO TO 17
32 WRITE(NPNT,39)(ITEMP(MZ),MZ=1,2)
GO TO 17
33 WRITE(NPNT,39)(ITEMP(MZ),MZ=1,3)
GO TO 17
34 WRITE(NPNT,39)(ITEMP(MZ),MZ=1,4)
GO TO 17

```

```
35      WRITE(NPPNT,39)(ITEMP(MZ),MZ=1,5)
36      GO TO 17
37      WRITE(NPRNT,39)(ITEMP(MZ),MZ=1,6)
38      GO TO 17
39      WRITE(NPRNT,39)(ITEMP(MZ),MZ=1,7)
        GO TO 17
38      WRITE(NPRNT,39)(ITEMP(MZ),MZ=1,8)
17      CONTINUE
39      FORMAT(27X,8I7)
        GO TO 15
5       CONTINUE
C       INFORMATION ABOUT LINKS
        WRITE(NPPNT,100)
100     FORMAT(//,15X,29HTRANSMISSION LINK INFORMATION,/,18X,4HLINK,
1      1 7X,5HLINES,6X,12HTIME BETWEEN,7X,9HBREAKDOWN,/,4IX,
2      2 9HBREAKDOWN,10X,8HDURATION)
        DO 109 I=1,NLINK
        READ(NCPDR,102)MLK(I),TBB(I),TOB(I)
102     FORMAT(15,F8.2,F8.3)
109     WRITE(NPRNT,101)MLK(I),TBB(I),TOB(I)
101     FORMAT(18X,14,7X,14,8X,F8.2,7X,F8.3)
        CALL GASP
        CALL EXIT
        END
```

```

SUBROUTINE EVNTS(IX)
DIMENSION NSET(10000)
COMMON QSET(10000)
COMMON/GCOM1/ATRIB(25), JEVNT, MFA, MFE(100), MLE(100), MSTOP,
1 NCRDP, NNAP0, NNAPT, NNAR, NNFIL, NNO(100), NNTRY, NPNRT, PP&RM(50,4),
2 TNOW, TTREG, TTCLR, TTFIN, TTRIB(25), TTSET
COMMON/UCHN/IRT(1500,8), MLK(100), NLK(100), LST(100), TBB(100),
1 TOB(100), PLACE(15,15), CARR(15), CDUR(15), PRI(15,5), ICA(15,15,5),
2 ICA(15,15,5), ICP(15,15,5), ICD(15,15,5), ICC(15,15,5),
3 IIRT(15,15,8), ITMP(8), NODES, NLINK, ZENG, STRST
EQUIVALENCE(NSET(1), QSET(1))
GO TO(101,102,103,104,105,106)IX
101 CALL GENCL
RETURN
102 CALL ENDL
RETURN
103 CALL LNKDN
RETURN
104 CALL LNKUP
RETURN
105 CALL TTST
RETURN
106 CALL ENSIM
RETURN
END

```

```

SUBROUTINE GENCL
DIMENSION NSET(10000)
COMMON/QSET(10000)
COMMON/GCOM1/ATRIB(25),JEVNT,MFA,MFE(100),MLF(100),MSTOP,
1 NCNDP,NNAP0,NNAP1,NNATR,NNFTL,NNQ(100),NNTRY,NPRNT,PPARM(50,4),
2 TNOW,TTBEG,TTCLR,TTFIN,TTIB(25),TTSET
COMMON/UCWN/IRT(500,8),MLK(100),NLK(100),LST(100),TRB(100),
1 TOR(100),PLACE(15,15),CARR(15),CDUR(15),PRI(15,5),ICA(15,15,5),
2 ICB(15,15,5),ICP(15,15,5),ICU(15,15,5),ICC(15,15,5),
3 IRT(15,15,8),ITEMP(8),NODES,NLINK,ZENGT,STRST
EQUIVALENCE(NSET(1),QSET(1))
C SCHEDULE NEXT CALL
II=ATRIB(3)
ATRIB(1)=TNOW+EXPON(CARR(II),1)
CALL FILEM(1)
RND=DRAND(5)
IP=IP+1
100 RND=RND-PRI(II,IP)
IF(RND.GT.0)GO TO 100
ATRIB(5)=IP
C DETERMINE SINK
RND=DRAND(5)
IJ=0
110 IJ=IJ+1
PNJ=PND-PLACE(II,IJ)
IF(PNJ.GT.0)GO TO 110
ATRIB(4)=IJ
ICA(II,IJ,IP)=ICA(II,IJ,IP)+1
C SEE IF ROUTE IS AVAILABLE
IZ=0
505 IZ=IZ+1
IF(IZ.GT.8)GO TO 1500
IF(IIRT(II,IJ,IZ).EQ.0)GO TO 1500
IR=IIRT(II,IJ,IZ)
IQ=0
600 IQ=IQ+1
IF(IQ.GT.8)GO TO 1000
IL=IRT(IR,IQ)
IF(IL.LE.0)GO TO 1000
IF(LST(IL).GT.0.5)GO TO 505
IF(NLK(IL).EQ.MLK(IL))GO TO 505
GO TO 600
C GOOD ROUTE FOUND. INCREMENT LINKS.
1000 IA=0
69 IA=IA+1
IF(IA.GT.8)GO TO 300
IAA=IRT(IR,IA)
IF(IAA.EQ.0)GO TO 300
NLK(IAA)=NLK(IAA)+1
GO TO 69
C SCHEDULE END OF CALL
300 ATRIB(1)=TNOW+EXPON(CDUR(II),1)
ATRIB(2)=2,
ATRIB(3)=II
ATRIB(4)=IJ
ATRIB(5)=IP
ATRIB(6)=IR
CALL FILEM(1)
RETURN
C DETERMINE IF JOB CAN BE PREEMPTED
1500 IF(IP.EQ.1)GO TO 1400
C SEARCH FILE
NEXT=MFE(1)
550 CALL COPY(NEXT)
NNEXT=NEXT+NNAP0
NNEXT=NSET(NNEXT)
IF(ATRIB(2).NE.2.)GO TO 900
JI=ATRIB(3)
JJ=ATRIB(4)
JP=ATRIB(5)
JR=ATRIB(6)
IF(J9.NE.IP)GO TO 900
IF(I1.NE.JI)GO TO 900
IF(IJ.NE.JJ)GO TO 900
IF(IP.GT.JP)GO TO 950
IF(NNEXT.EQ.0)GO TO 1400
800

```

```
NEXT=NNEXT
GO TO 550
REMOVE ENTRY
950 CALL PMOVE(NEXT,1)
ICP(II,IJ,JP)=ICP(II,IJ,JP)+1
ATTRIB(5)=IP
ATTRIB(1)=TNOW+EXPON(CARR(II),1)
CALL FILEM(1)
RETURN
1400 ICD(II,IJ,IP)=ICB(II,IJ,IP)+1
PRETURN
END
```

```

SUBROUTINE ENDCL
DIMENSION NSET(10000)
COMMON QSET(10000)
COMMON/GCO4/ATRIB(25),JEVNT,MFA,MFE(100),MLE(100),MSTOP,
1 NCORDR,NNAPD,NNAPL,NNATR,NNFIL,NNQ(100),NNTRY,NPRNT,PPARM(50,4),
2 TNOW,TTBEG,TTCLR,TTFIN,TTRI(25),TTSET
COMMON/UOWNIRT(500,8),NLK(100),NLK(100),LST(100),TBB(100),
1 TOB(100),PLACE(15,15),CARR(15),COJR(15),PRI(15,5),ICA(15,15,5),
2 ICB(15,15,5),ICP(15,15,5),ICO(15,15,5),ICC(15,15,5),
3 IIRT(15,15,8),ITEMP(8),NODES,NLINK,ZENGT,STRST
EQUIVALENCE(NSET(1),QSET(1))
C RECODED COMPLETED CALL
II=ATRIB(3)
IJ=ATRIB(4)
IP=ATRIB(5)
IR=ATRIB(6)
ICC(II,IJ,IP)=ICC(II,IJ,IP)+1
C RELEASE LINKS
IX=1
7 IF(IX.GT.8)GO TO 100
IF(IR(I9,IX).EQ.0)GO TO 100
IZ=IRT(IR,IX)
NLK(IZ)=NLK(IZ)-1
IX=IX+1
GO TO 7
CONTINUE
RETURN
END

```

```

SUBROUTINE LNKDN
DIMENSION NSET(10000)
COMMON/QSET(10000)
COMMON/GCOM/ATRIB(25),JEVNT,MFA,MFE(100),MLE(100),MSTOP,
1 NCRDR,NNAP0,NNAP1,NNATR,NNFIL,NNQ(100),NNTRY,NPRNT,PPARM(50,4),
2 TNOW,TTBEG,TTCLR,TTFIN,TTRIB(25),TTSET
COMMON/UCWN/IRT(500,8),MLK(100),NLK(100),LST(100),TBB(100),
1 TOR(100),PLACE(15,15),CARR(15),CDUR(15),PRI(15,5),ICA(15,15,5),
2 ICB(15,15,5),ICP(15,15,5),ICD(15,15,5),ICC(15,15,5),
3 IIRT(15,15,8),ITEMP(8),NODES,NLINK,ZENGT,STRSF
EQUIVALENCE(NSET(1),QSET(1))
C SCHEDULE LINK DOWN
JJ=ATRIB(3)
LST(JJ)=1
C SCHEDULE END OF BREAKDOWN
ATRIB(1)=TNOW+EXPON(TOR(JJ),3)
ATRIB(2)=4.
CALL FILEM(1)
C DETERMINE IF CALL WILL BE LOST. STEP THROUGH FILE 1.
NEXT=MFE(1)
50 CALL COPY(NEXT)
NNEXT=NEXT+NNAP0
NNEXT=NSET(NNEXT)
IF(ATRIB(2).NE.2.)GO TO 100
II=ATRIB(3)
IJ=ATRIB(4)
IP=ATRIB(5)
IR=ATRIB(6)
C CHECK ROUTE TO SEE IF CALL IS LOST
IX=1
20 IF((X.GT.8)GO TO 100
IF(IRT(IR,IX).EQ.0)GO TO 100
IF(IRT(IR,IX).EQ.JJ)GO TO 200
IX=IX+1
GO TO 20
C LINK FOUND. DECREASE OTHER LINKS.
200 IX=1
IF((X.GT.8)GO TO 201
IZ=IRT(IR,IX)
IF(IIZ.EQ.0)GO TO 201
NLK(I2)=NLK(IZ)-1
IX=IX+1
GO TO 30
C REMOVE CALL AND RECORD DROPPED CALL
201 ICN(II,IJ,IP)=ICD(II,IJ,IP)+1
CALL RMVME(NEXT,1)
C FIND NEXT ENTRY
100 IF(NNEXT.EQ.0)GO TO 400
NEXT=NNEXT
GO TO 50
400 NLK(JJ)=0
RETURN
END

```

```

SUBROUTINE LNKUP
DIMNSION NSET(10000)
COMMON QSET(10000)
COMMON/GCOM1/ATRIB(25),JEVNT,MFA,MFE(100),MLE(100),MSTOP,
1 NCPDR,NNAPL,NNAPT,NNATR,NNFIL,NNQ(100),NNTRY,NPRNT,PPARM(50,4),
2 TNOW,TTBEG,TTCLR,TTFIN,TTRIB(25),TSET
COMMON/UCHN/IRT( 500,8),MLK(100),NLK(100),LST(100),TBB(100),
1 TOR(100),PLACE(15,15),CRR(15),COUR(15),PRT(15,5),ICA(15,15,5),
2 ICB(15,15,5),ICP(15,15,5),ICD(15,15,5),ICC(15,15,5),
3 IIRT(15,15,8),ITEMP(8),NODES,NLINK,ZENGT,STRST
EQUIVALENCE(NSET(1),QSET(1))
C SCHEDULE NEXT BREAKDOWN
JJ=ATRIB(3)
ATRIB(1)=TNOW+EXPON(TBB(JJ),1)
ATRIB(2)=3.0
CALL FILEM(1)
CHANGE STATUS OF LINK
LST(JJ)=0
RETURN
END

```

```

SUBROUTINE ITTST
DIMENSION NSET(10000)
COMMON/QSET(10000)
COMMON/GCOM1/ATRIB(25),JEVNT,MFA,MFE(100),MLE(100),MSTOP,
1 NCRDR,NNAPO,NNAPT,NNATR,NNFTL,NNO(100),NNTRY,NPRNT,PPARM(50,4),
2 TNOW,TTBEG,TTCLR,TTFIN,TRIB(25),TTSET
COMMON/UCWN/IRT(.500,.8),MLK(100),NLK(100),LST(100),TRB(100),
1 TOR(100),PLACE(15,15),CARR(15),COUR(15),PZI(15,5),ICA(15,15,5),
2 ICR(15,15,5),ICP(15,15,5),ICD(15,15,5),ICC(15,15,5),
3 IIRT(15,15,8),ITEMP(8),NODES,NLINK,ZENGT,STRST
EQUIVALENCE(NSET(1),QSET())
C INITIALIZE ROUTE STATISTICS
DO 1 I=1,NODES
DO 1 J=1,NODES
DO 1 K=1,5
ICA(I,J,K)=ICA(I,J,K)-ICB(I,J,K)-ICB(I,J,K)-ICD(I,J,K)-ICP(I,J,K)
ICB(I,J,K)=0
ICB(I,J,K)=0
ICD(I,J,K)=0
ICC(I,J,K)=0
1 RETURN
END

```

```

SUBROUTINE ENSIM
DIMENSION NSET(10000)
COMMON QSET(10000)
COMMON /COM1/ATRIB(25),JEVNT,MFA,MFE(100),MLE(100),MSTOP,
1 NCRDR,NNAPO,NNAPT,NNATR,NNFIL,NNQ(100),NNTRY,NPRNT,PPARM(50,4),
2 TNOW,TBEG,TCLR,TFIN,TTRIB(25),TSET
COMMON /UCWN/IIRL(500,8),MLK(100),NLK(100),LST(100),TBB(100),
1 TDL(100),PLACE(15,15),CARR(15),CDUR(15),PRI(15,5),ICA(15,15,5),
2 ICB(15,15,5),ICP(15,15,5),ICD(15,15,5),ICC(15,15,5),
3 IIRL(15,15,8),ITEMP(8),NODES,NLINK,ZENGT,STRST
EQUIVALENCE(INSET(1),QSET(1))
FORMAT(//,30X,39HOUTPUT OF SWITCHING CIRCUIT PERFORMANCE./)
FORMAT(10X,6HSOURCE,6X,6HSINK,4X,8HPRIORITY,10X,6HSTATUS,10X,
1 3HOPS,9X,10HPROPORTION)
FORMAT(/,10X,I4,7X,I4,8X,I3,5X,15HCALLS ATTEMPTED,9X,I6,5X,F6.4)
FORMAT(4IX,15HCALLS COMPLETED,9X,I6,5X,F6.4)
FORMAT(4IX,13HCALLS BLOCKED,11X,I6,5X,F6.4)
FORMAT(4IX,13HCALLS DROPPED,11X,I6,5X,F6.4)
FORMAT(4IX,15HCALLS PREEMPTED,9X,I6,5X,F6.4)
FORMAT(4IX,17HCALLS IN PROGRESS,7X,I6,5X,F6.4)
DO 9 II=1,NODES
DO 9 IJ=1,NODES
DO 9 IP=1,5
IF(II,FO,IJ)GO TO 9
ISUM=ICC(II,IJ,IP)+ICB(II,IJ,IP)+ICD(II,IJ,IP)+ICP(II,IJ,IP)
IREM=ICA(II,IJ,IP)-ISUM
PZ=FLOAT(ICA(II,IJ,IP))
PA=1.00
PC=FLOAT(ICC(II,IJ,IP))/PZ
PB=FLOAT(ICB(II,IJ,IP))/PZ
PD=FLOAT(ICD(II,IJ,IP))/PZ
PP=FLOAT(ICP(II,IJ,IP))/PZ
PR=FLOAT(IREM)/PZ
WRITE(NPRNT,1)
MSTOP=-1
WRITE(NPRNT,2)
WRITE(NPRNT,3) II,IJ,IP,ICA(II,IJ,IP),PA
WRITE(NPRNT,4) ICC(II,IJ,IP),PC
WRITE(NPRNT,5) ICB(II,IJ,IP),PB
WRITE(NPRNT,6) ICD(II,IJ,IP),PD
WRITE(NPRNT,7) ICP(II,IJ,IP),PP
WRITE(NPRNT,8) IREM,PR
9 CONTINUE
RETURN
ENJ

```

```

SUBROUTINE INTLC
DIMENSION NSET(10000)
COMMON QSET(10000)
COMMON/GCOM1/ATRIB(25),JEVNT,MFA,MFE(100),MLE(100),MSTOP,
1 NCRDR,NNAPL,NNAPT,NNATR,NNFIL,NNOT100),NNTRY,NPRNT,PPARM(50,4),
2 TNOW,TTBEG,TTCLR,TTFIN,TTRIB(25),TTSET
COMMON/UOWN/IRT(500,8),MLK(100),NLK(100),LST(100),TBB(100),
1 TOB(100),PLACE(15,15),CARR(15),CDUR(15),PRI(15,5),ICA(15,15,5),
2 ICB(15,15,5),ICP(15,15,5),ICO(15,15,5),ICC(15,15,5),
3 IIRT(15,15,8),ITEMP(8),NODES,NLINK,ZENGT,STRST
EQUIVALENCE (NSET(1),QSET(1))
ATRIB(4)=0.
ATRIB(5)=0.
ATRIB(6)=0.
C   INITIALIZE LINK INFORMATION AND BREAKDOWNS
DO 3 I=1,NLINK
NLK(I)=0
LST(I)=0
ATRIB(1)=EXPON(TBB(1),1)
ATRIB(2)=3.0
ATRIB(3)=1
3 CALL FILEM(1)
C   INITIALIZE DEMAND FOR CALLS
DO 2 J=1,NODES
ATRIB(1)=EXPON(CARR(J),2)
ATRIB(2)=1.
ATRIB(3)=J
2 CALL FILEM(1)
C   INITIALIZE STATISTICS VARIABLES
DO 1 I=1,NODES
DO 1 J=1,NODES
DO 1 K=1,5
ICA(I,J,K)=0
ICB(I,J,K)=0
ICP(I,J,K)=0
ICO(I,J,K)=0
1 ICC(I,J,K)=0
ATRIB(1)=STRST
ATRIB(2)=5.
ATRIB(3)=0
CALL FILEM(1)
C   SCHEDULE END OF SIMULATION
ATRIB(1)=STRST+ZENGT
ATRIB(2)=6.
CALL FILEM(1)
RETURN
END

```

**Sample Output from GASP-IV Program**

**APPENDIX G**

CALLS FROM SOURCE 1

AVERAGE TIME BETWEEN CALLS .25000

AVERAGE DURATION OF CALL .40000

PROBABILITY OF PRIORITY 1 CALLS IS .750  
PROBABILITY OF PRIORITY 2 CALLS IS .050  
PROBABILITY OF PRIORITY 3 CALLS IS .100  
PROBABILITY OF PRIORITY 4 CALLS IS .050  
PROBABILITY OF PRIORITY 5 CALLS IS .050

PROBABILITY OF A CALL GOING TO SINK 2 IS .400  
ROUTES IN ORDER OF PREFERENCE

1  
4      7  
9      3      2

PROBABILITY OF A CALL GOING TO SINK 3 IS .400  
ROUTES IN ORDER OF PREFERENCE

1      2  
4      5      3  
8

PROBABILITY OF A CALL GOING TO SINK 5 IS .200  
ROUTES IN ORDER OF PREFERENCE

4  
1      2      6

CALLS FROM SOURCE 2

AVERAGE TIME BETWEEN CALLS .50000

AVERAGE DURATION OF CALL .50000

PROBABILITY OF PRIORITY 1 CALLS IS .900  
PROBABILITY OF PRIORITY 2 CALLS IS .050  
PROBABILITY OF PRIORITY 3 CALLS IS .050  
PROBABILITY OF PRIORITY 4 CALLS IS -.000  
PROBABILITY OF PRIORITY 5 CALLS IS -.000

PROBABILITY OF A CALL GOING TO SINK 1 IS .200  
ROUTES IN ORDER OF PREFERENCE

1  
4      7  
9      3      2

PROBABILITY OF A CALL GOING TO SINK 3 IS .400  
ROUTES IN ORDER OF PREFERENCE

2  
7      6

PROBABILITY OF A CALL GOING TO SINK 4 IS .300  
ROUTES IN ORDER OF PREFERENCE

2        3  
7        5  
1        8        3  
7        4        9

PROBABILITY OF A CALL GOING TO SINK 5 IS .100  
ROUTES IN ORDER OF PREFERENCE  
7

CALLS FROM SOURCE 3

AVERAGE TIME BETWEEN CALLS .10000

AVERAGE DURATION OF CALL .30000

PROBABILITY OF PRIORITY 1 CALLS IS .500  
PROBABILITY OF PRIORITY 2 CALLS IS .200  
PROBABILITY OF PRIORITY 3 CALLS IS .100  
PROBABILITY OF PRIORITY 4 CALLS IS .100  
PROBABILITY OF PRIORITY 5 CALLS IS .100

PROBABILITY OF A CALL GOING TO SINK 1 IS .100  
ROUTES IN ORDER OF PREFERENCE

8  
6        4

PROBABILITY OF A CALL GOING TO SINK 2 IS .300  
ROUTES IN ORDER OF PREFERENCE

2  
6        4  
3        5        4  
6        7        1

PROBABILITY OF A CALL GOING TO SINK 4 IS .300  
ROUTES IN ORDER OF PREFERENCE

3  
2        1        9

PROBABILITY OF A CALL GOING TO SINK 5 IS .300  
ROUTES IN ORDER OF PREFERENCE

8        9  
6

CALLS FROM SOURCE 4

AVERAGE TIME BETWEEN CALLS .20000

AVERAGE DURATION OF CALL .20000

PROBABILITY OF PRIORITY 1 CALLS IS .600  
PROBABILITY OF PRIORITY 2 CALLS IS .300  
PROBABILITY OF PRIORITY 3 CALLS IS .050  
PROBABILITY OF PRIORITY 4 CALLS IS .030  
PROBABILITY OF PRIORITY 5 CALLS IS .020

PROBABILITY OF A CALL GOING TO SINK 1 IS .300  
ROUTES IN ORDER OF PREFERENCE

9  
3     6     4  
5     7

PROBABILITY OF A CALL GOING TO SINK 2 IS .300  
ROUTES IN ORDER OF PREFERENCE

9     1  
3     2  
5     7  
5     6     2

PROBABILITY OF A CALL GOING TO SINK 3 IS .200  
ROUTES IN ORDER OF PREFERENCE

9     8  
9     1     2  
5     4     8  
5     4     1     2  
5     6  
5     7     2  
3

PROBABILITY OF A CALL GOING TO SINK 5 IS .200  
ROUTES IN ORDER OF PREFERENCE

5

CALLS FROM SOURCE 5

AVERAGE TIME BETWEEN CALLS .50000

AVERAGE DURATION OF CALL .60000

PROBABILITY OF PRIORITY 1 CALLS IS .400  
PROBABILITY OF PRIORITY 2 CALLS IS .300  
PROBABILITY OF PRIORITY 3 CALLS IS .100  
PROBABILITY OF PRIORITY 4 CALLS IS .150  
PROBABILITY OF PRIORITY 5 CALLS IS .050

PROBABILITY OF A CALL GOING TO SINK 1 IS .400  
ROUTES IN ORDER OF PREFERENCE

4  
7     1  
5     3     2     1

PROBABILITY OF A CALL GOING TO SINK 2 IS .400  
ROUTES IN ORDER OF PREFERENCE  
5 9 1  
7  
6 2

PROBABILITY OF A CALL GOING TO SINK 3 IS .100  
ROUTES IN ORDER OF PREFERENCE  
6

PROBABILITY OF A CALL GOING TO SINK 4 IS .100  
ROUTES IN ORDER OF PREFERENCE  
4 9  
4 8 3  
5  
6 3  
7 2 8 9

TRANSMISSION LINK INFORMATION

LINK	LINES	TIME BETWEEN BREAKDOWN	BREAKDOWN DURATION
1	5	40.00	2.000
2	6	60.00	.900
3	7	60.00	.500
4	4	90.00	1.500
5	3	100.00	1.000
6	6	40.00	.500
7	7	30.00	1.000
8	10	200.00	4.000
9	4	50.00	.500

OUTPUT OF SWITCHING CIRCUIT PERFORMANCE

SOURCE	SINK	PRIORITY	STATUS	OBS	PROPORTION
3	5	1	CALLS ATTEMPTED	150	1.0000
			CALLS COMPLETED	106	.7067
			CALLS BLOCKED	24	.1600
			CALLS DROPPED	1	.0067
			CALLS PREEMPTED	15	.1000
			CALLS IN PROGRESS	4	.0267

OUTPUT OF SWITCHING CIRCUIT PERFORMANCE

SOURCE	SINK	PRIORITY	STATUS	OBS	PROPORTION
3	5	2	CALLS ATTEMPTED	65	1.0000
			CALLS COMPLETED	58	.8788
			CALLS BLOCKED	4	.0615
			CALLS DROPPED	2	.0303
			CALLS PREEMPTED	2	.0303
			CALLS IN PROGRESS	0	.0000

OUTPUT OF SWITCHING CIRCUIT PERFORMANCE

SOURCE	SINK	PRIORITY	STATUS	OBS	PROPORTION
3	5	3	CALLS ATTEMPTED	39	1.0000
			CALLS COMPLETED	29	.9333
			CALLS BLOCKED	1	.0333
			CALLS DROPPED	1	.0333
			CALLS PREEMPTED	0	.0000
			CALLS IN PROGRESS	0	.0000

OUTPUT OF SWITCHING CIRCUIT PERFORMANCE

SOURCE	SINK	PRIORITY	STATUS	OBS	PROPORTION
3	5	4	CALLS ATTEMPTED	27	1.0000
			CALLS COMPLETED	26	.9630
			CALLS BLOCKED	0	.0000
			CALLS DROPPED	0	.0000
			CALLS PREEMPTED	0	.0000
			CALLS IN PROGRESS	1	.0370

OUTPUT OF SWITCHING CIRCUIT PERFORMANCE

SOURCE	SINK	PRIORITY	STATUS	OBS	PROPORTION
3	5	5	CALLS ATTEMPTED	24	1.0000
			CALLS COMPLETED	23	.9583
			CALLS BLOCKED	0	.0000
			CALLS DROPPED	1	.0417
			CALLS PREEMPTED	0	.0000
			CALLS IN PROGRESS	0	.0000

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